

# Survey of Ballistic Lunar Transfers to Near Rectilinear Halo Orbit

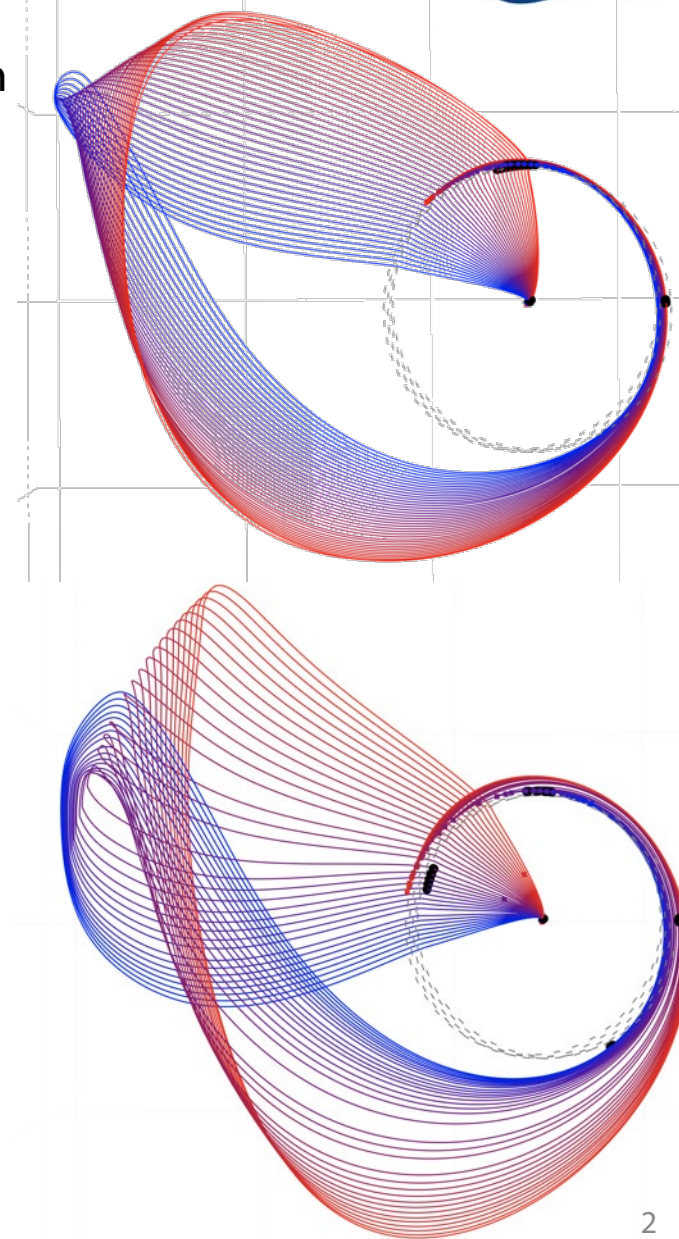
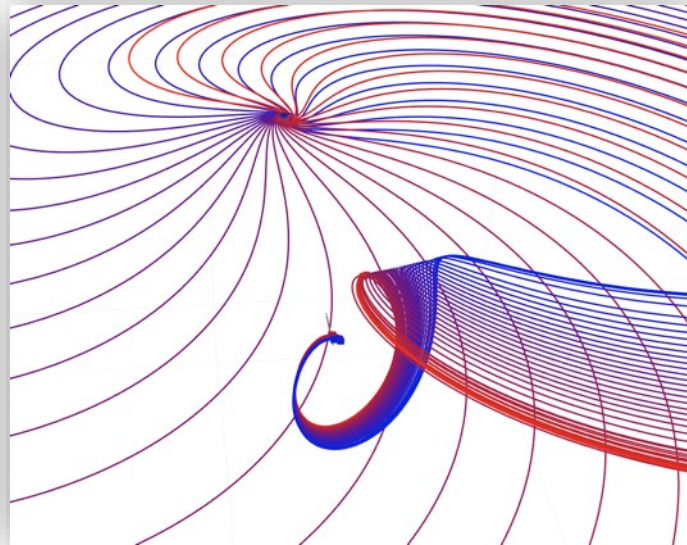
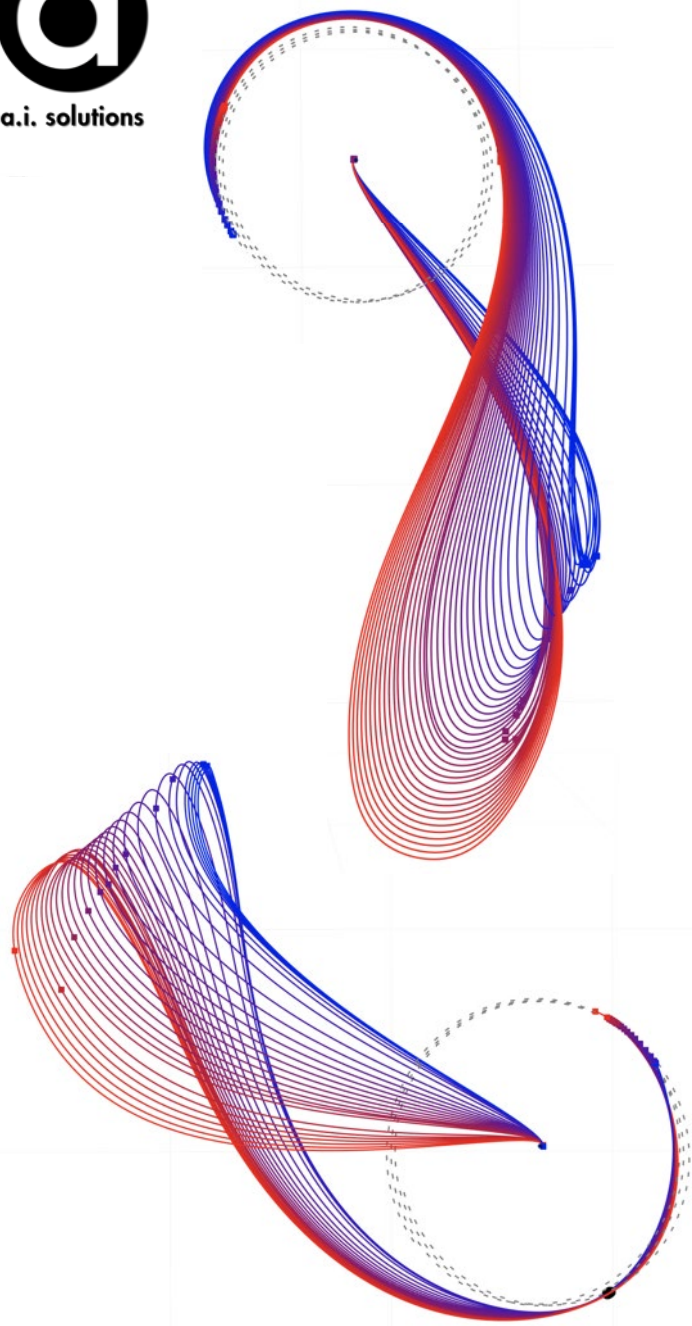
Nathan L. Parrish, Ethan Kayser, Shreya Udupa, Jeffrey S. Parker,  
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Goal: Evaluate and understand the trade space for ballistic lunar transfers from Earth launch to arrival in a near rectilinear halo orbit (NRHO).

Several favorable families were identified and studied.

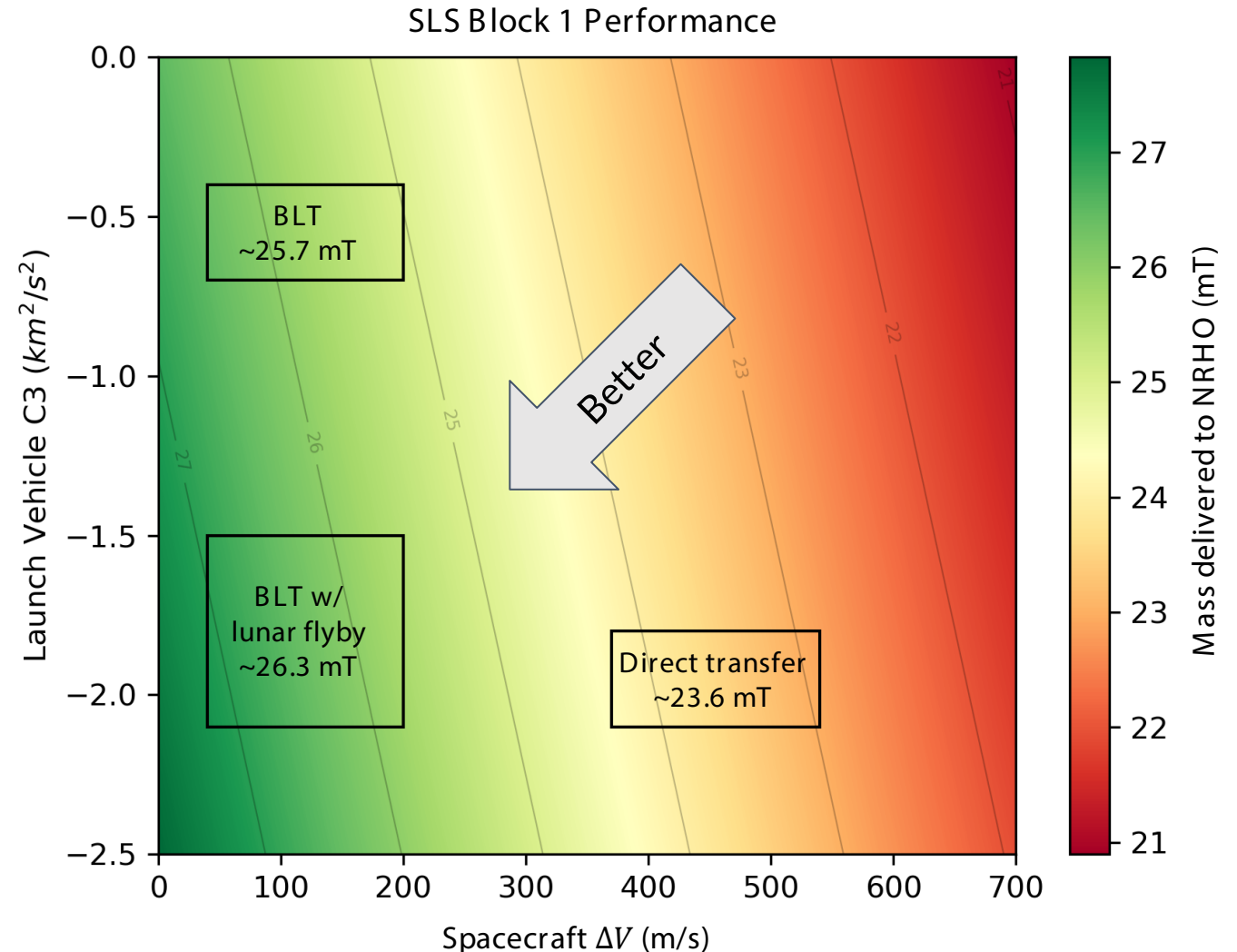
Over 70,000 optimal trajectories were designed in order to understand the trade space.



# Why Ballistic Lunar Transfer (BLT)?

- Assume spacecraft  $I_{sp} = 300$  s
- Benefits:
  - Reduced spacecraft  $\Delta V$
  - Reduced operational cadence (more time between maneuvers)
  - Increased launch window
  - Secondary payloads to anywhere in cislunar space
- Trade-offs:
  - Increased time of flight (12-20 weeks)
  - Greater maximum distance from Earth can challenge comms
  - Increased operations duration
  - Potentially higher  $C_3$

**Bottom line:**  
Increased mass delivered to NRHO



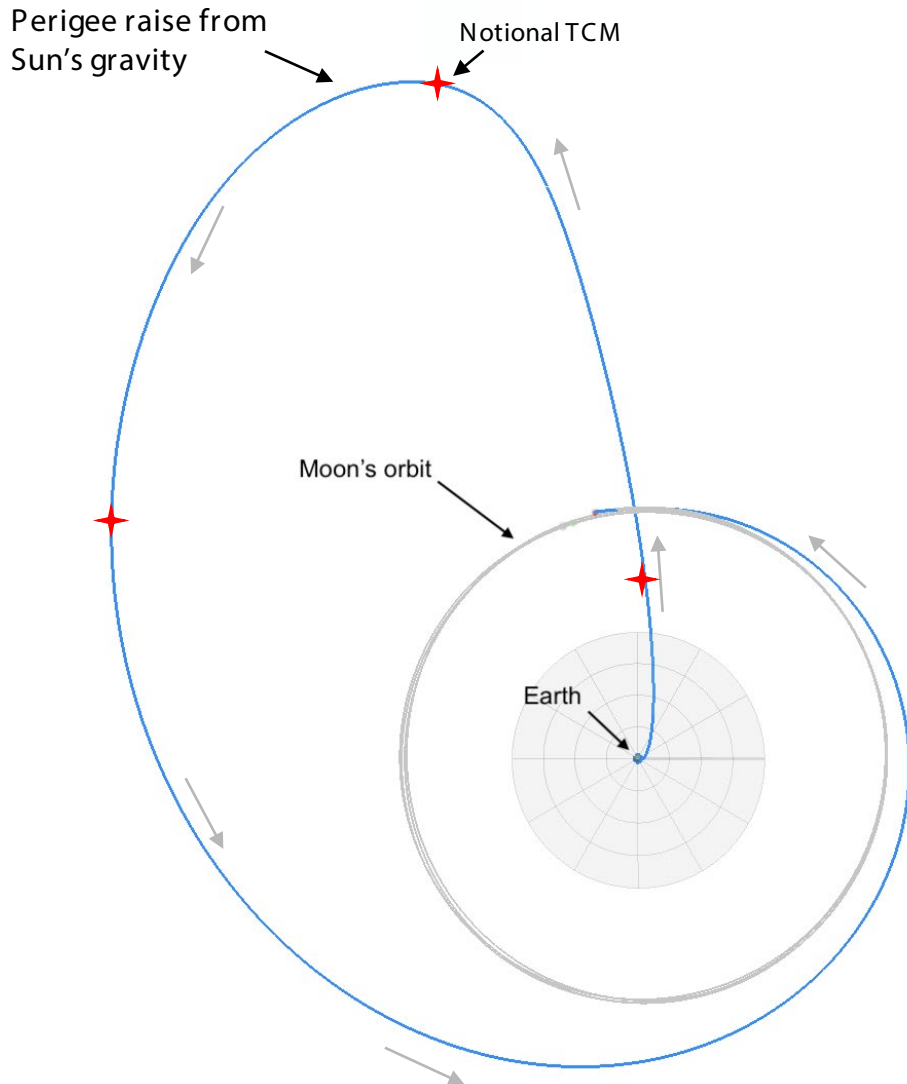
A large, detailed image of the Moon's surface, showing craters and lunar maria, occupies the left side of the slide.

# Introduction & Background

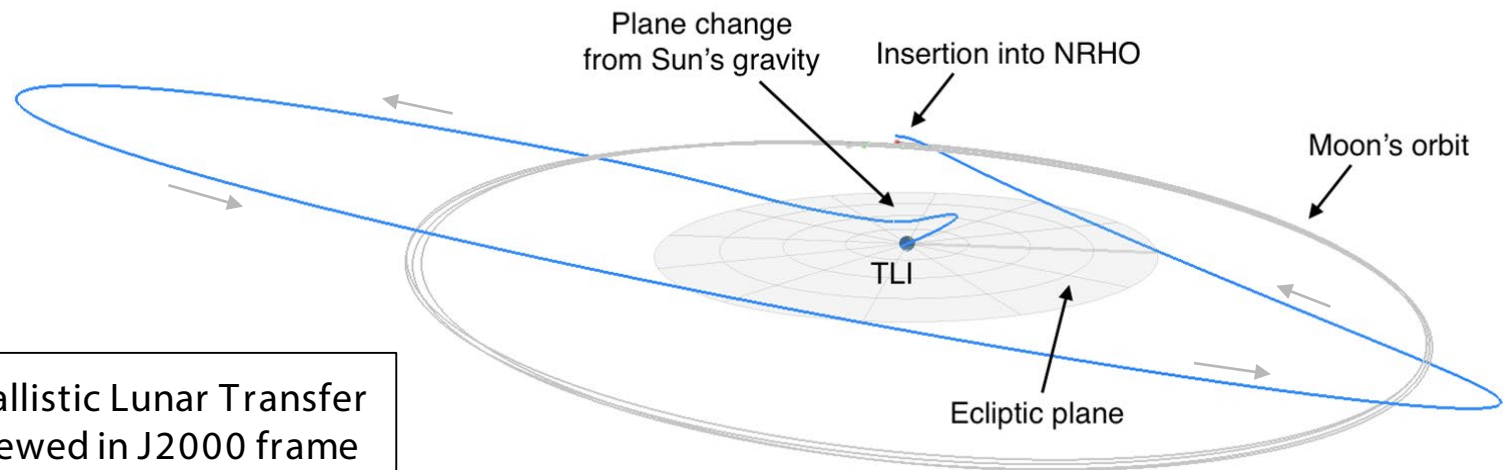


# Background - BLTs

- Sun's gravity causes plane change and perigee raise, taking the spacecraft from TLI to NRHO for "free"
- Deterministic  $\Delta V$  opens up launch period and permits rendezvous with target
- Transfer relies on dynamics of four-body problem (Earth, Sun, Moon, spacecraft)



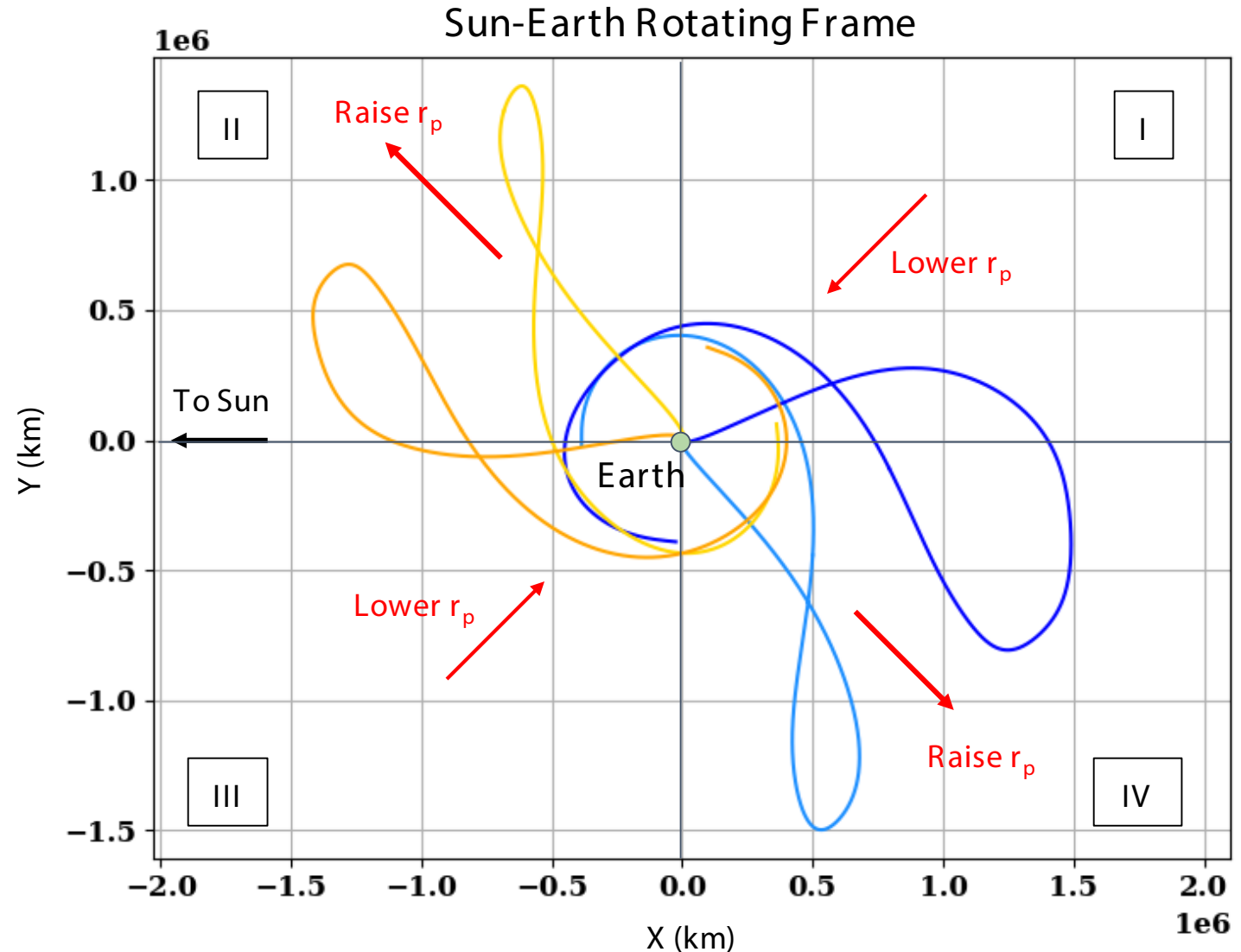
Ballistic Lunar Transfer  
viewed in J2000 frame



# Background - BLTs



- Sun's gravity perturbation affects the radius of perigee
- Effect determined by which quadrant apogee is in:
  - Quadrants II or IV raise perigee
  - Quadrants I or III lower perigee



## Dynamics and Assumptions —Phase-Fixed (Gateway Rendezvous)

- Simulation engine: Copernicus Trajectory Design and Optimization System
- Force model:
  - Sun, Earth and Moon point masses, states from DE430
  - 14,000 kg spacecraft
  - SRP Area: 23 m<sup>2</sup>, CR: 2.0, spherical model
  - Impulsive maneuvers
- Launch not considered —start in parking orbit at Earth
  - 100 km circular
  - 28° inclination
  - Node orientation optimized
- NRHO: 9:2 patch point from CR3BP
- Maneuvers:
  - Trans Lunar Injection (TLI): Velocity direction
  - Up to 3 Deep Space Maneuvers (DSMs)
  - NRHO Insertion near perilune with 0-rev “wind on”
- Objective: Minimize weighted sum of spacecraft  $\Delta V$  and TLI  $\Delta V$  (TLI  $\Delta V$  included for lunar flyby cases only)

## Dynamics and Assumptions —Phase-Fixed (Gateway Rendezvous)

- Simulation engine: Copernicus Trajectory Design and Optimization System
- Force model:
  - Sun & Earth point masses, states from DE430
  - **Moon 8x8 gravity field, GRGM660PRIM model**
  - 14,000 kg spacecraft
  - SRP Area: 23 m<sup>2</sup>, CR: 2.0, spherical model
  - Impulsive maneuvers
- Launch not considered —start in parking orbit at Earth
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- NRHO: rendezvous with reference NRHO
- Maneuvers:
  - Trans Lunar Injection (TLI): Velocity direction
  - Up to 3 Deep Space Maneuvers (DSMs)
  - **Several options examined for NRHO insertion and rendezvous**
- Objective: Minimize weighted sum of spacecraft  $\Delta V$  and TLI  $\Delta V$  (TLI  $\Delta V$  included for lunar flyby cases only)



A large, detailed image of the Moon's surface, showing craters and lunar features, occupies the left side of the slide.

# Results

	Phase-Free (NRHO perilune can occur at any epoch)	Phase-Fixed (Rendezvous with reference NRHO)
No lunar flyby	For 4 families of transfers, studied: <ul style="list-style-type: none"> <li>• Day-to-day variation</li> <li>• Month-to-month variation</li> <li>• Eclipses during transfer</li> </ul>	For 4 families of transfers, studied: <ul style="list-style-type: none"> <li>• Day-to-day variation</li> <li>• Month-to-month variation</li> <li>• 6 options for insertion &amp; rendezvous</li> </ul>
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# Families of Transfers

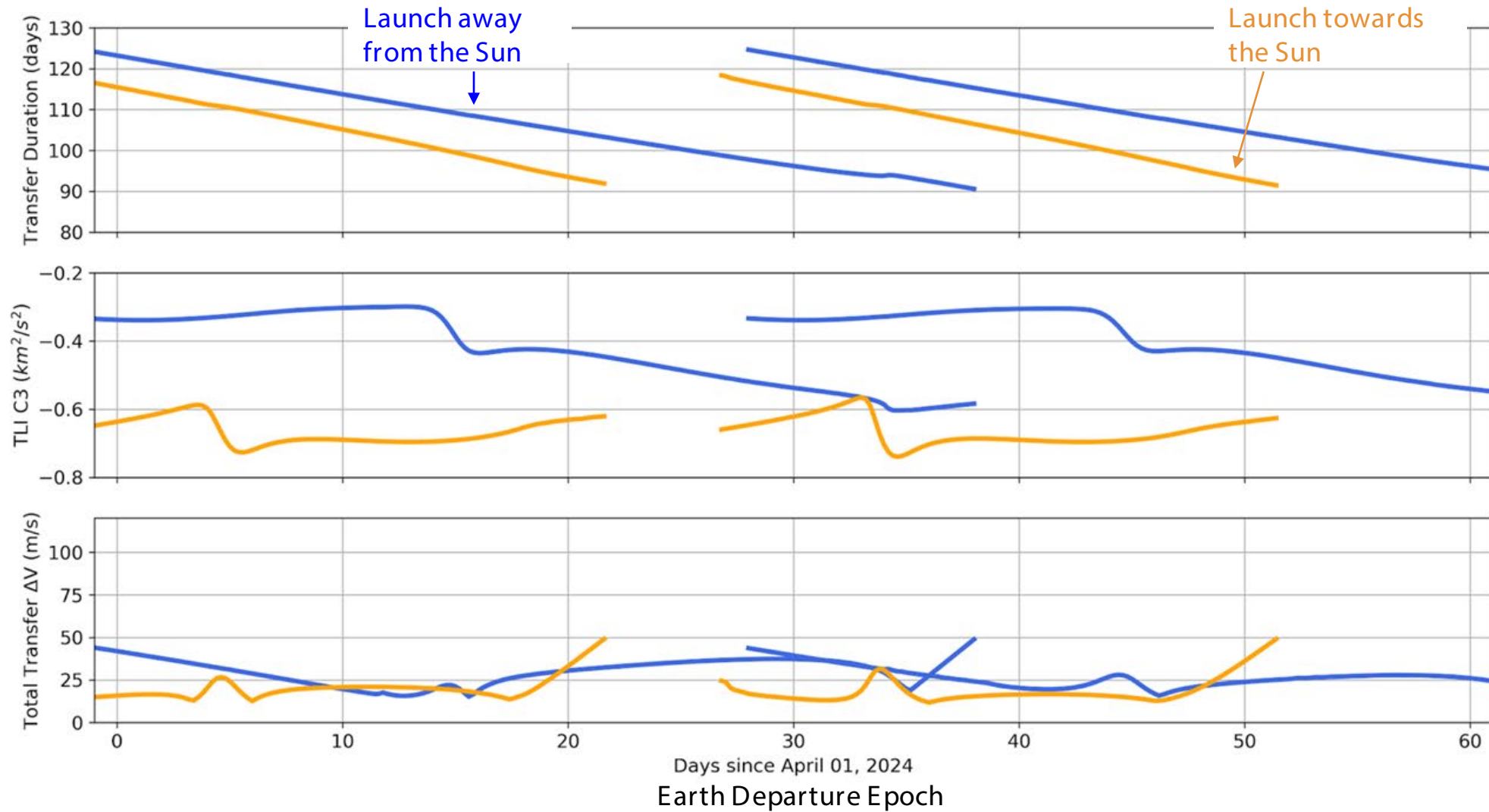
- Many families of transfers exist.
- This is a partial taxonomy.
- Each of these “families” has numerous “sub-families”, many of which are practically equivalent.

## See reference:

Parker J.S., “Families of Low-Energy Lunar Halo Transfers”, Advances in the Astronautical Sciences, 2006.

#	Lunar flyby	Apogee quadrant	TLI approx. location	# of Moon orbits between flyby & insertion
1	No	II (towards Sun)	Ascending node	N/A
2	No	II (towards Sun)	Descending node	N/A
3	No	IV (away from Sun)	Ascending node	N/A
4	No	IV (away from Sun)	Descending node	N/A
5	Yes	II (towards Sun)	Ascending node	4
6	Yes	II (towards Sun)	Ascending node	5
7	Yes	II (towards Sun)	Ascending node	5-6
8	Yes	IV (away from Sun)	Ascending node	4
9	Yes	IV (away from Sun)	Ascending node	5
10	Yes	IV (away from Sun)	Ascending node	5-6
11	Yes	II (towards Sun)	Descending node	4
12	Yes	II (towards Sun)	Descending node	5
13	Yes	II (towards Sun)	Descending node	5-6
14	Yes	IV (away from Sun)	Descending node	4
15	Yes	IV (away from Sun)	Descending node	5
16	Yes	IV (away from Sun)	Descending node	5-6

# Phase-Free BLTs - TLI near Ascending Node





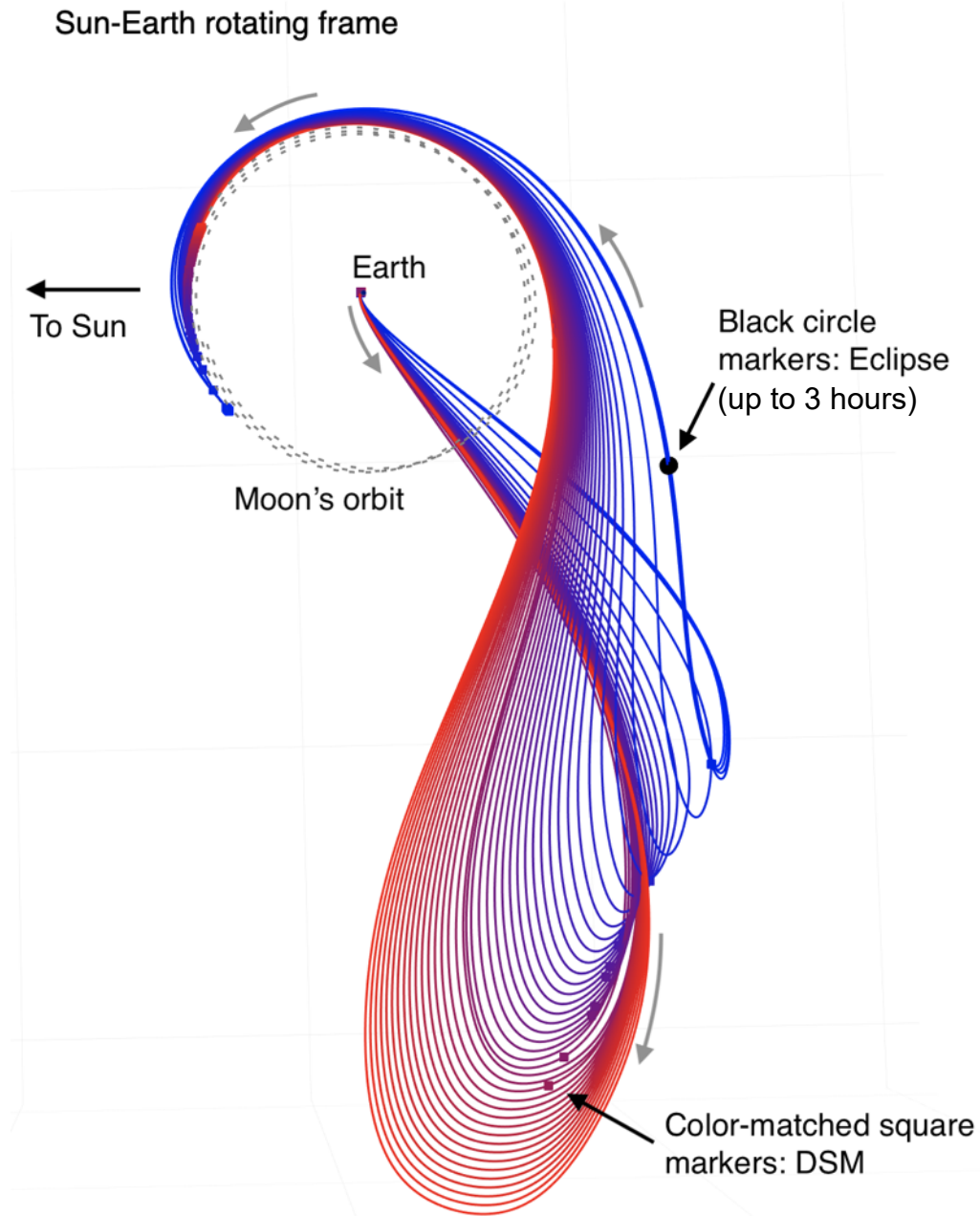
# Phase-Free BLTs

Launch into quadrant IV  
(away from Sun)

Launch dates:  
March 30, 2024 – May 9, 2024

Family repeats every synodic  
month

Transfer time 85-125 days



- Launch 2024 MAR 30 12:00:00.000
- Launch 2024 MAR 31 12:00:00.000
- Launch 2024 APR 01 12:00:00.000
- Launch 2024 APR 02 12:00:00.000
- Launch 2024 APR 03 12:00:00.000
- Launch 2024 APR 04 12:00:00.000
- Launch 2024 APR 05 12:00:00.000
- Launch 2024 APR 06 12:00:00.000
- Launch 2024 APR 07 12:00:00.000
- Launch 2024 APR 08 12:00:00.000
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- Launch 2024 APR 10 12:00:00.000
- Launch 2024 APR 11 12:00:00.000
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- Launch 2024 APR 26 12:00:00.000
- Launch 2024 APR 27 12:00:00.000
- Launch 2024 APR 28 12:00:00.000
- Launch 2024 APR 29 12:00:00.000
- Launch 2024 APR 30 12:00:00.000
- Launch 2024 MAY 01 12:00:00.000
- Launch 2024 MAY 02 12:00:00.000
- Launch 2024 MAY 03 12:00:00.000
- Launch 2024 MAY 04 12:00:00.000
- Launch 2024 MAY 05 12:00:00.000
- Launch 2024 MAY 06 12:00:00.000
- Launch 2024 MAY 07 12:00:00.000
- Launch 2024 MAY 08 12:00:00.000
- Launch 2024 MAY 09 12:00:00.000
- ..... Moon's orbit

# Phase-Free BLTs

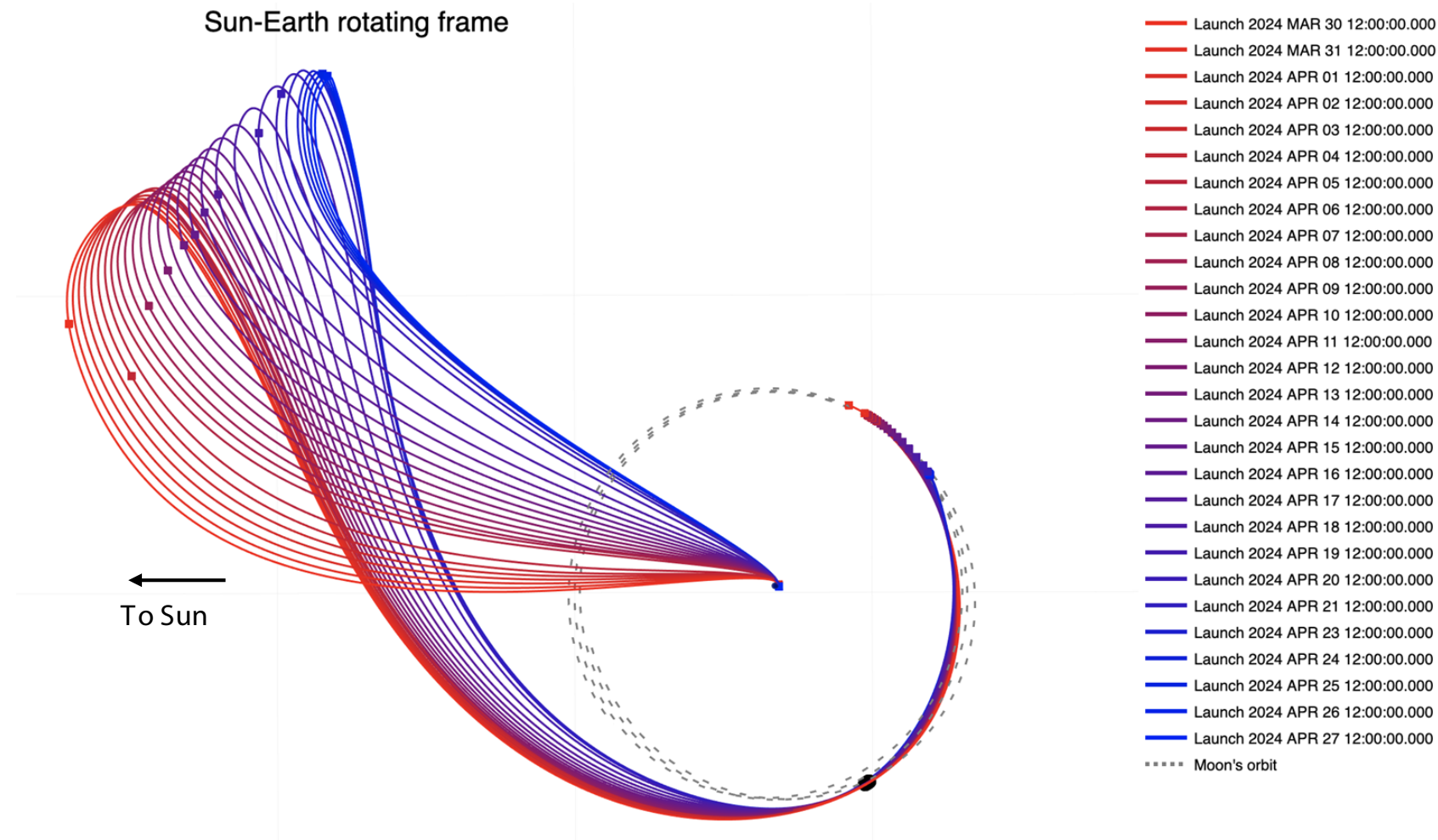


Launch into quadrant II  
(towards Sun)

Launch dates:  
March 30, 2024 – April 27, 2024

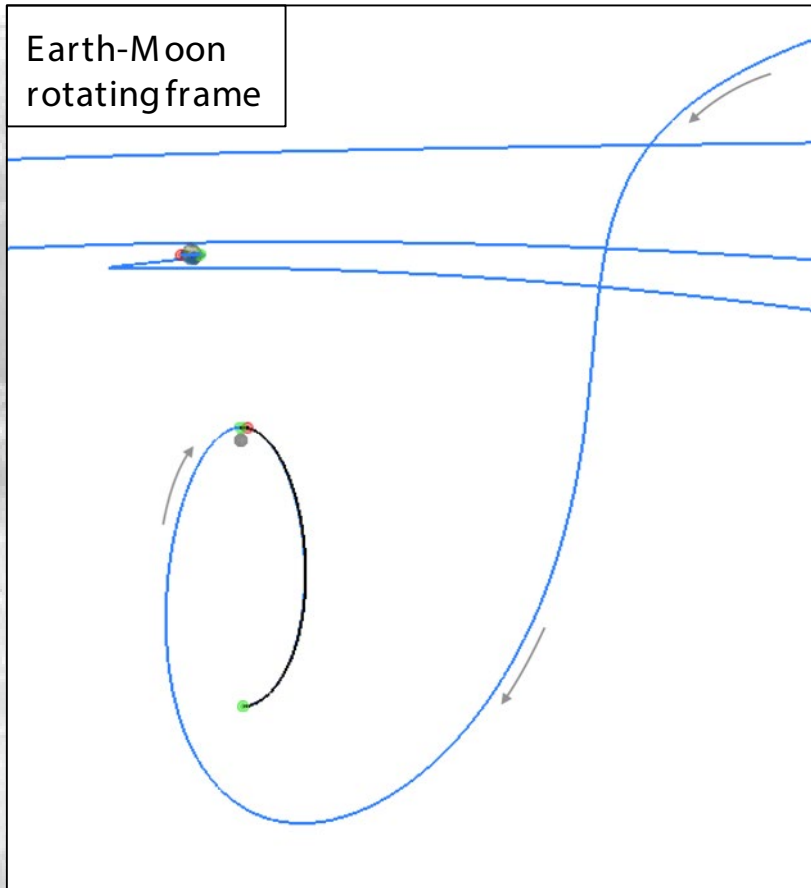
Family repeats every synodic  
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Transfer time 85-125 days



	Phase-Free (NRHO perilune can occur at any epoch)	Phase-Fixed (Rendezvous with reference NRHO)
No lunar flyby	For 4 families of transfers, studied: <ul style="list-style-type: none"> <li>• Day-to-day variation</li> <li>• Month-to-month variation</li> <li>• Eclipses during transfer</li> </ul>	For 4 families of transfers, studied: <ul style="list-style-type: none"> <li>• Day-to-day variation</li> <li>• Month-to-month variation</li> <li>• 6 options for insertion &amp; rendezvous</li> </ul>
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# Phase-Fixed BLTs (Gateway Rendezvous)



## Questions:

- How does deterministic spacecraft  $\Delta V$  change as a function of launch date and arrival date?
- When considering rendezvous with reference Gateway orbit, how are launch periods affected?

## Notes:

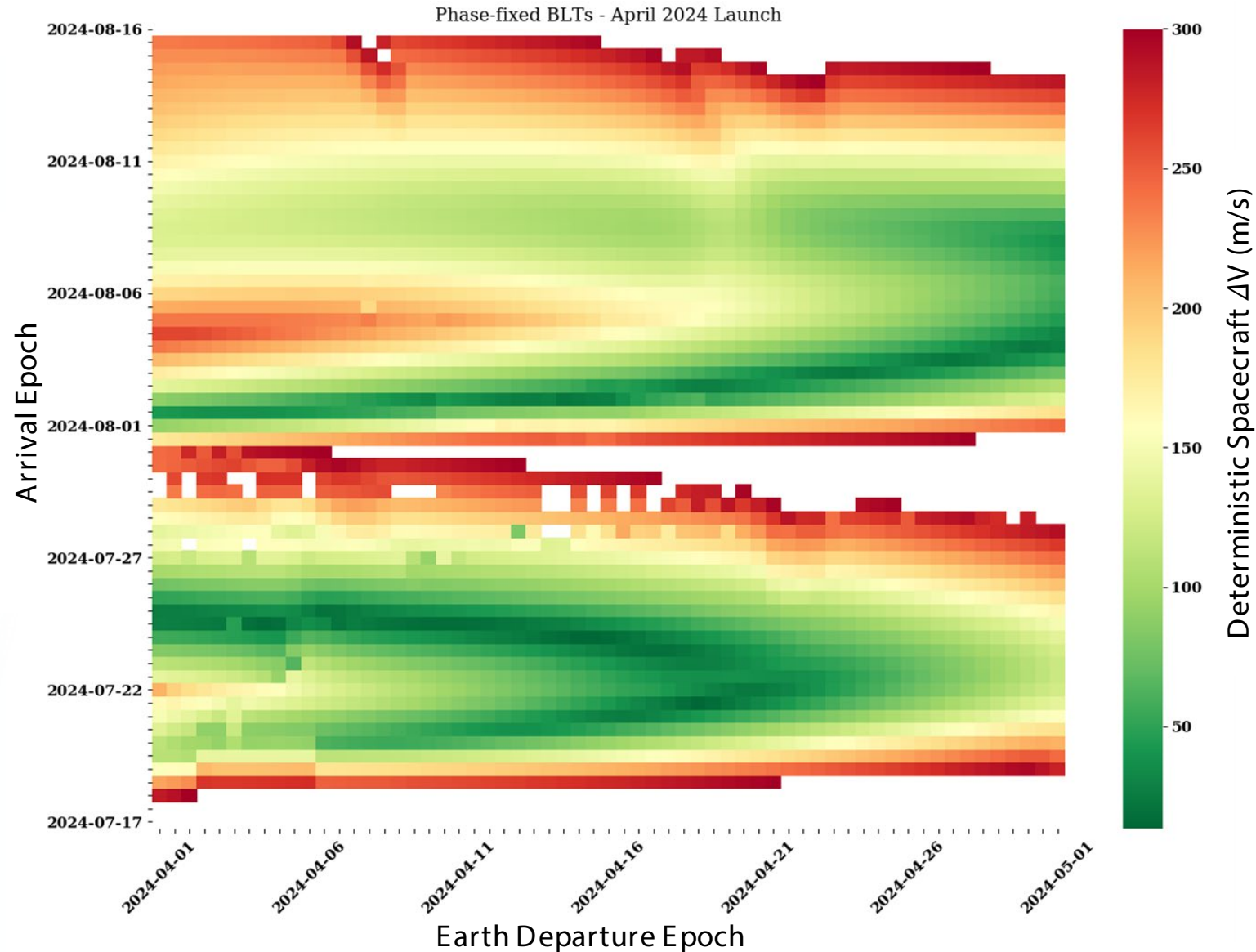
- Assume insertion into NRHO always occurs at perilune
- For phase-free cases, perilune insertion can take place at any epoch
- For phase-fixed cases, perilune insertion must take place at ~same epoch as Gateway perilune



# Phase-Fixed BLTs (Gateway Rendezvous)

Launch away from Sun

Launch towards Sun

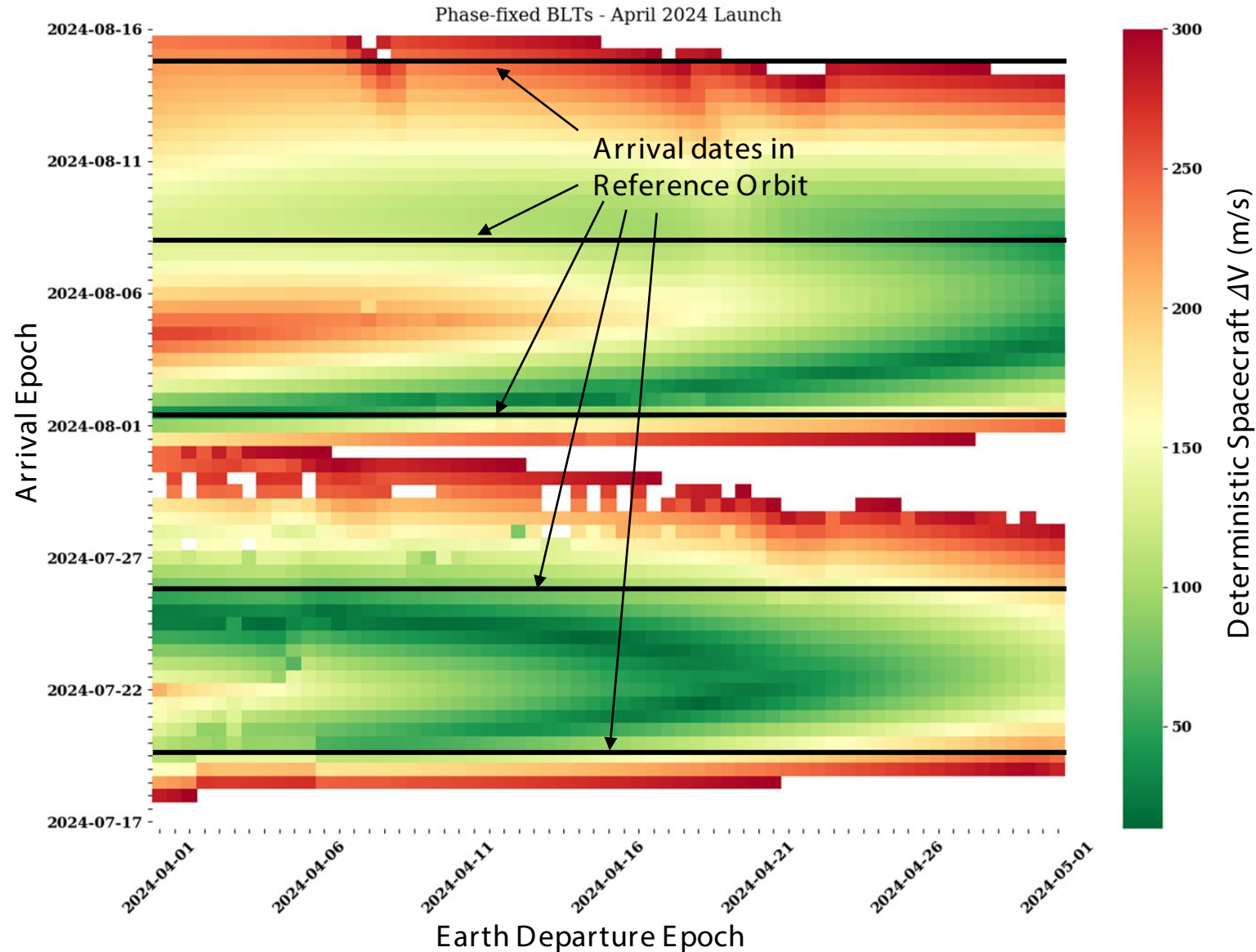




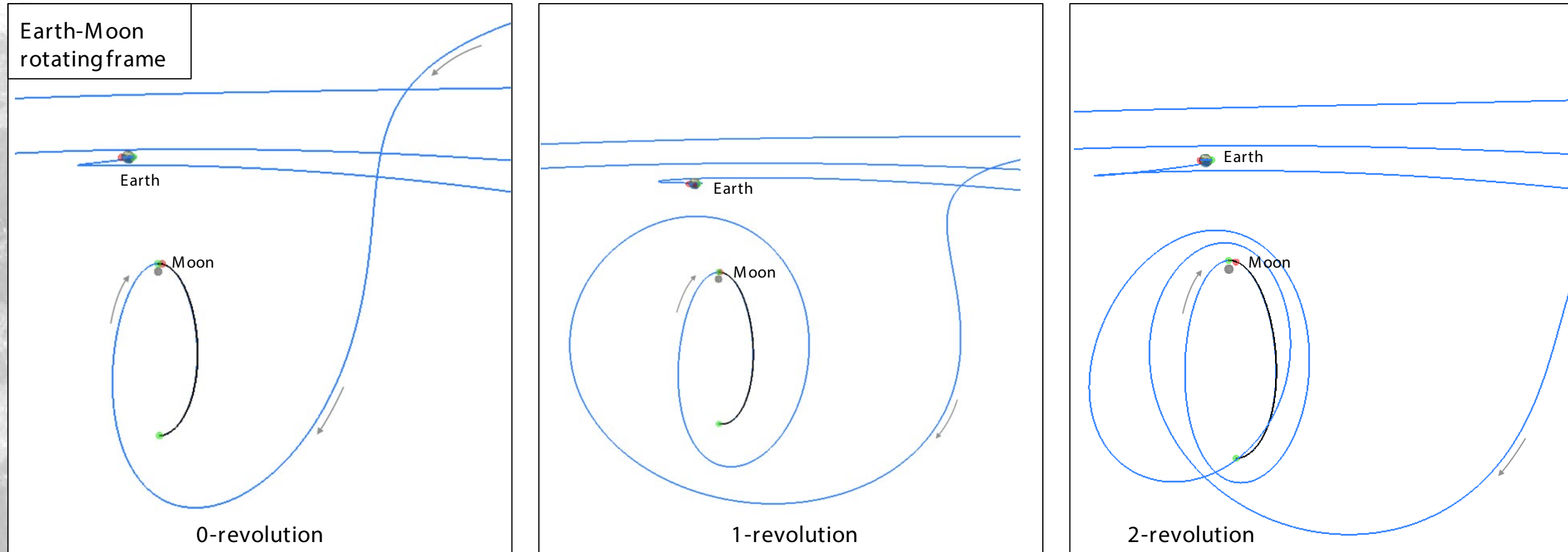
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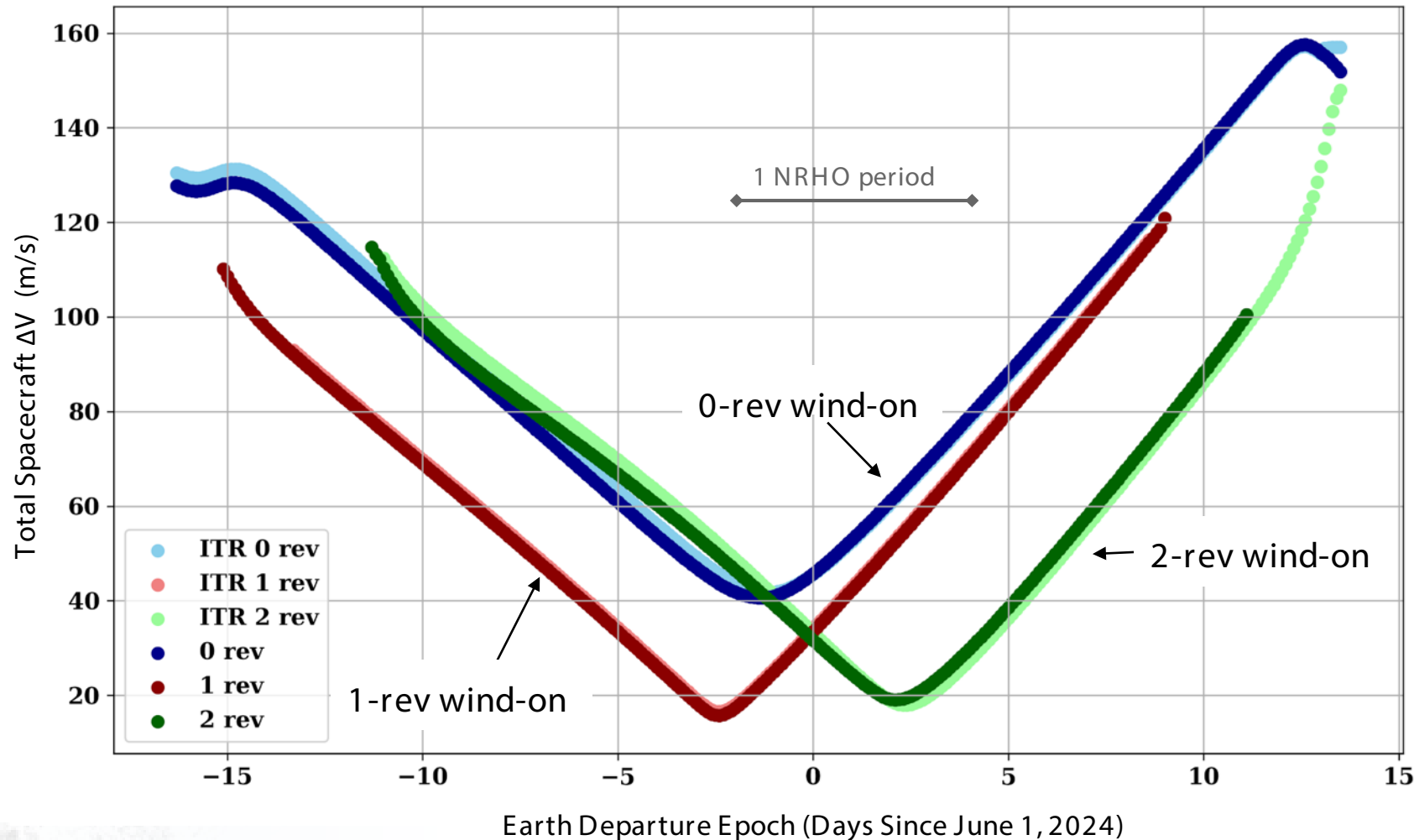


# Insertion & Rendezvous Study



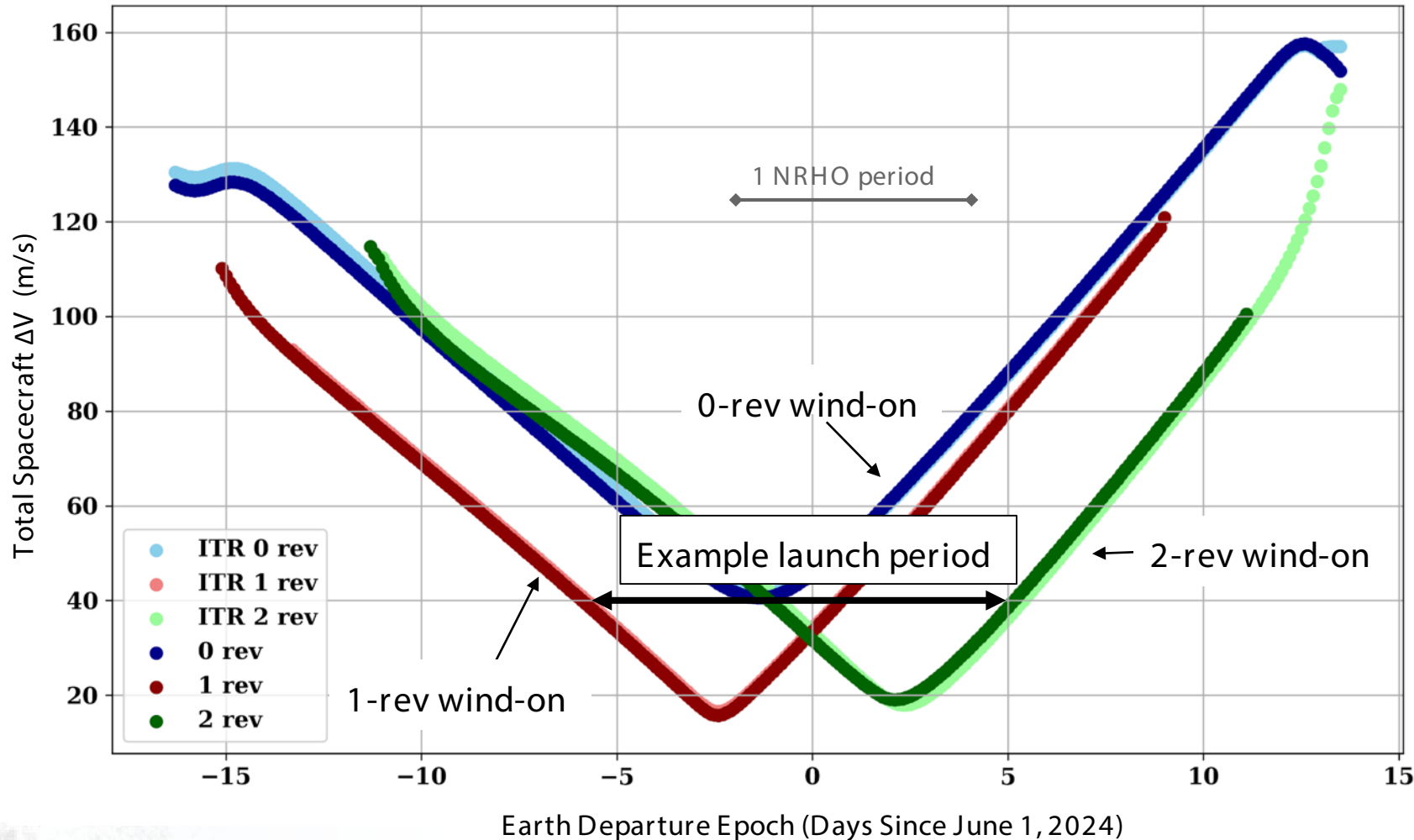
Increasing the number of revolutions of “wind-on” reduces deterministic insertion  $\Delta V$  at the expense of time of flight.

# Insertion & Rendezvous Study



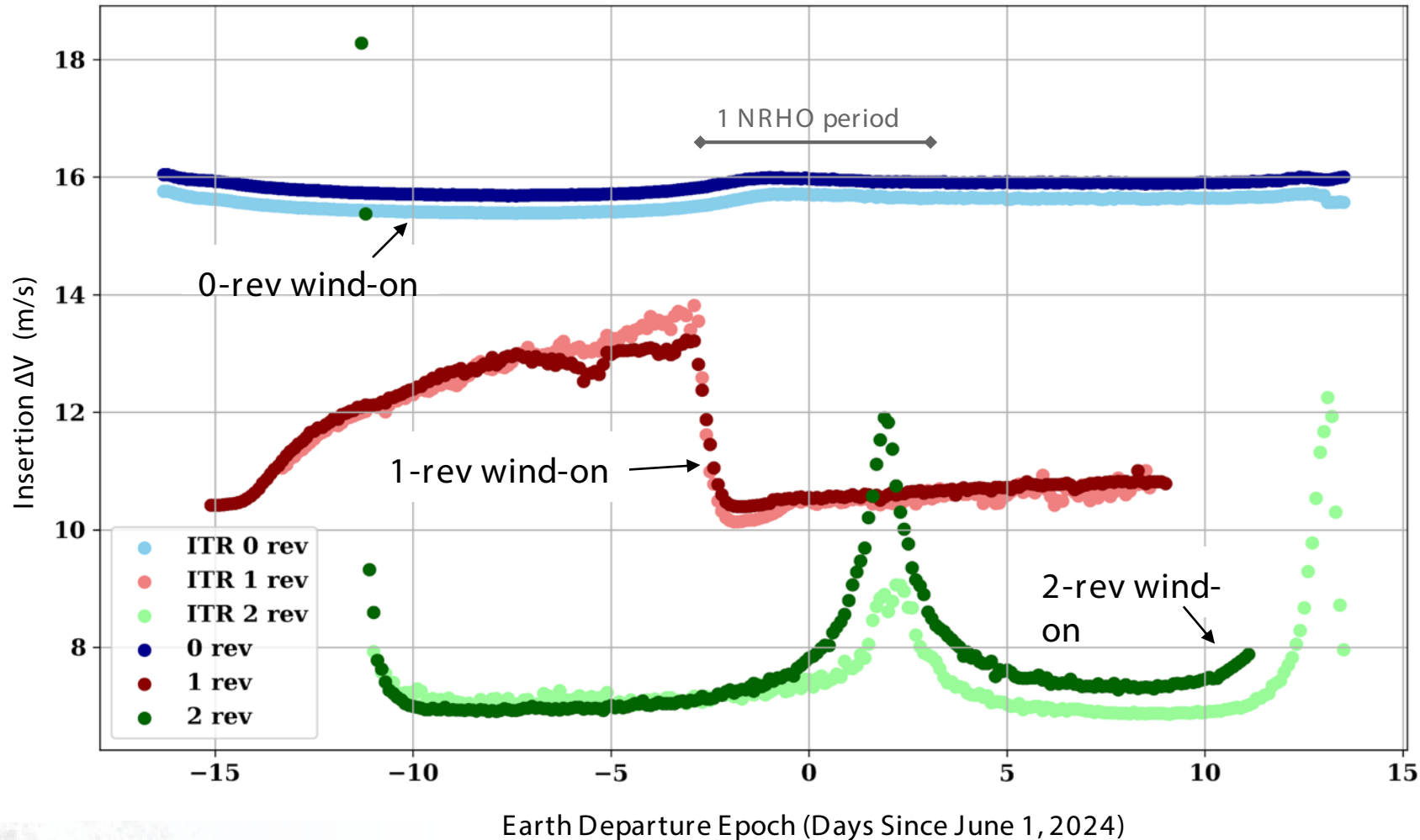
- Most  $\Delta V$  is in the DSMs

# Insertion & Rendezvous Study



- Most  $\Delta V$  is in the DSMs
- Launch period can be extended by 4-5 days by choosing different wind-on durations

# Insertion & Rendezvous Study



- In general, adding revolutions to the arrival wind-on reduces the insertion  $\Delta V$ .

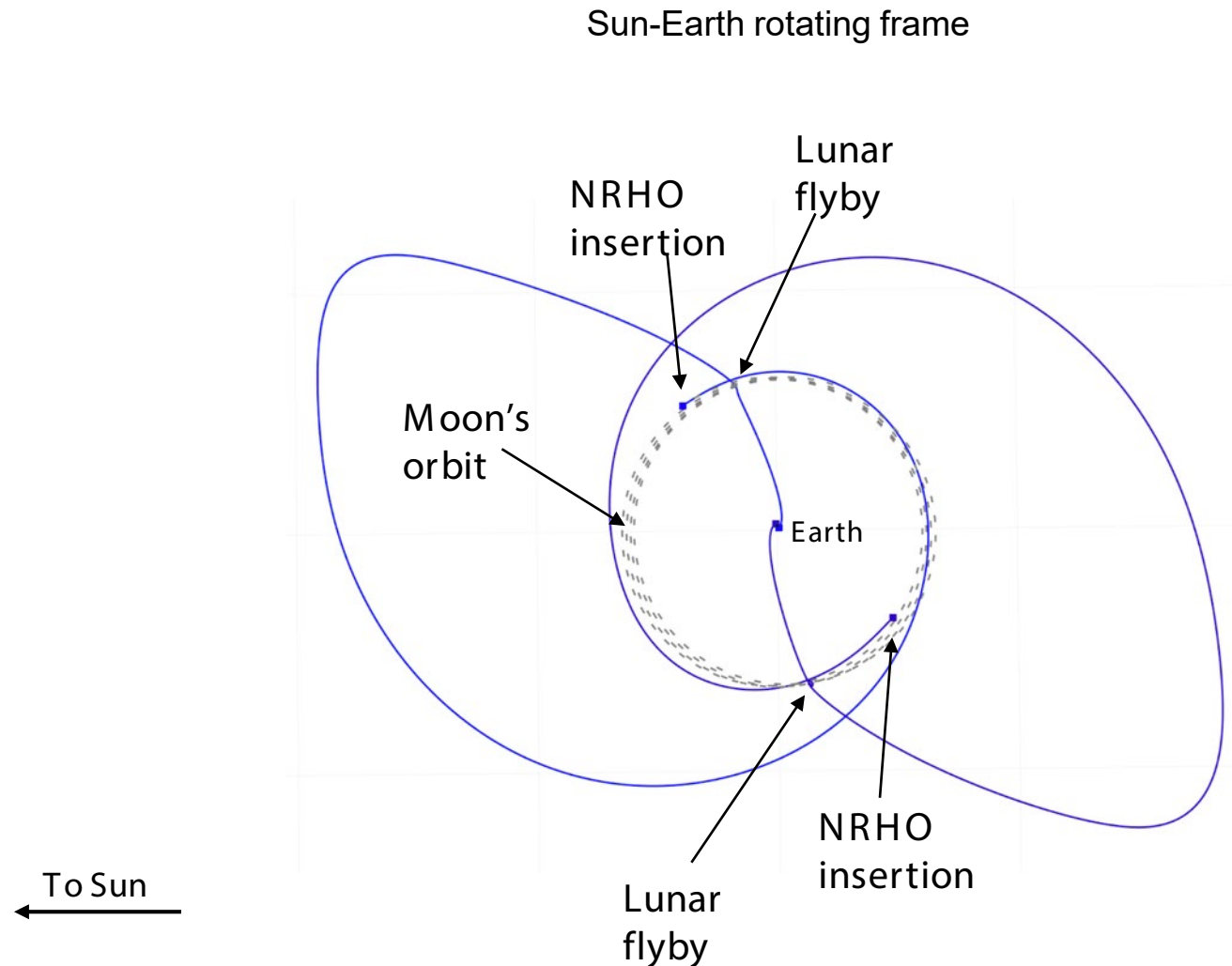


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# Phase-Free BLTs with Lunar Flyby



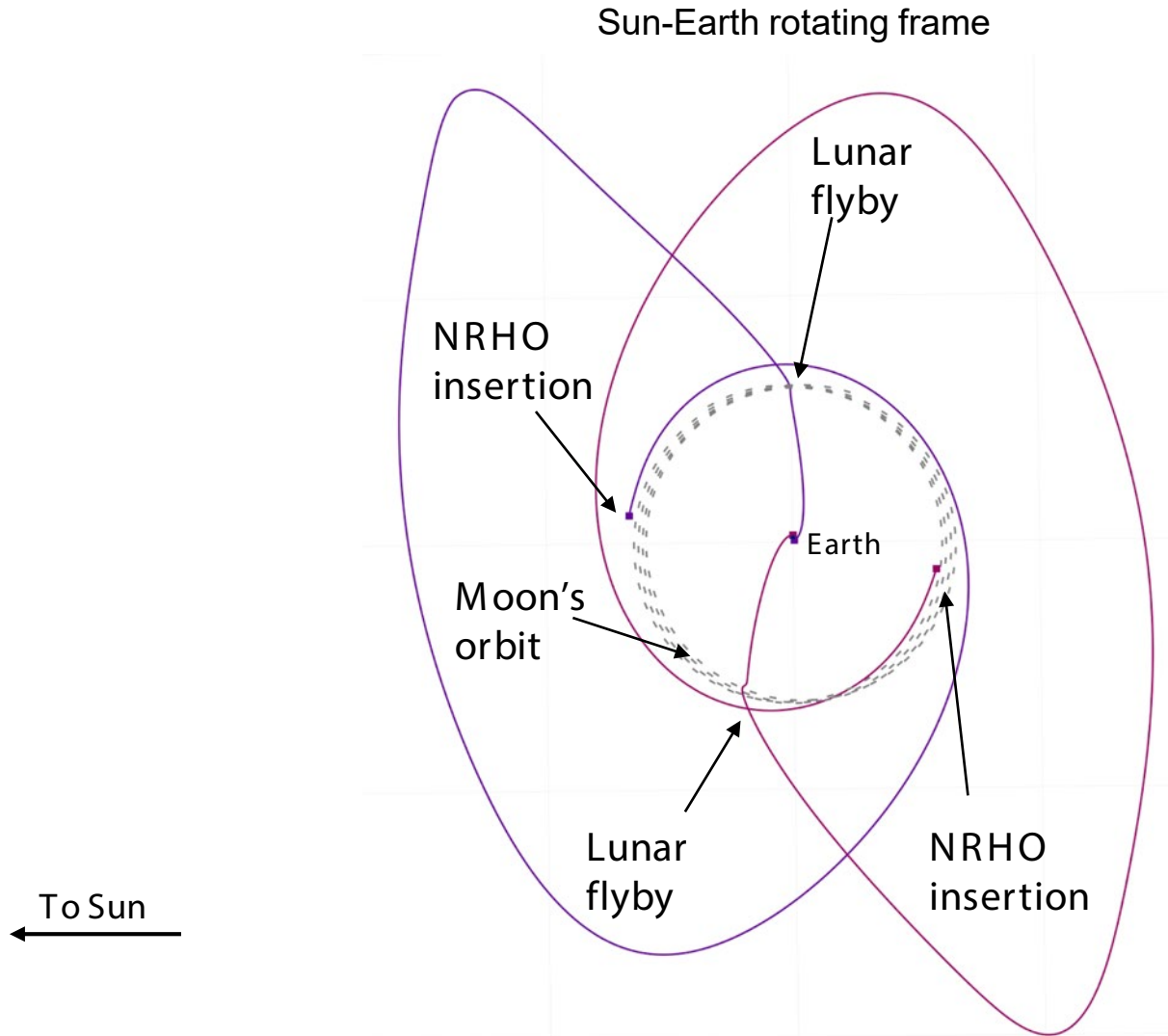
- Outbound lunar flyby reduces launch vehicle C3 requirement
- Additional geometry constraint introduced —reduces launch period
- Transfer options come in pairs every month



# Phase-Free BLTs with Lunar Flyby



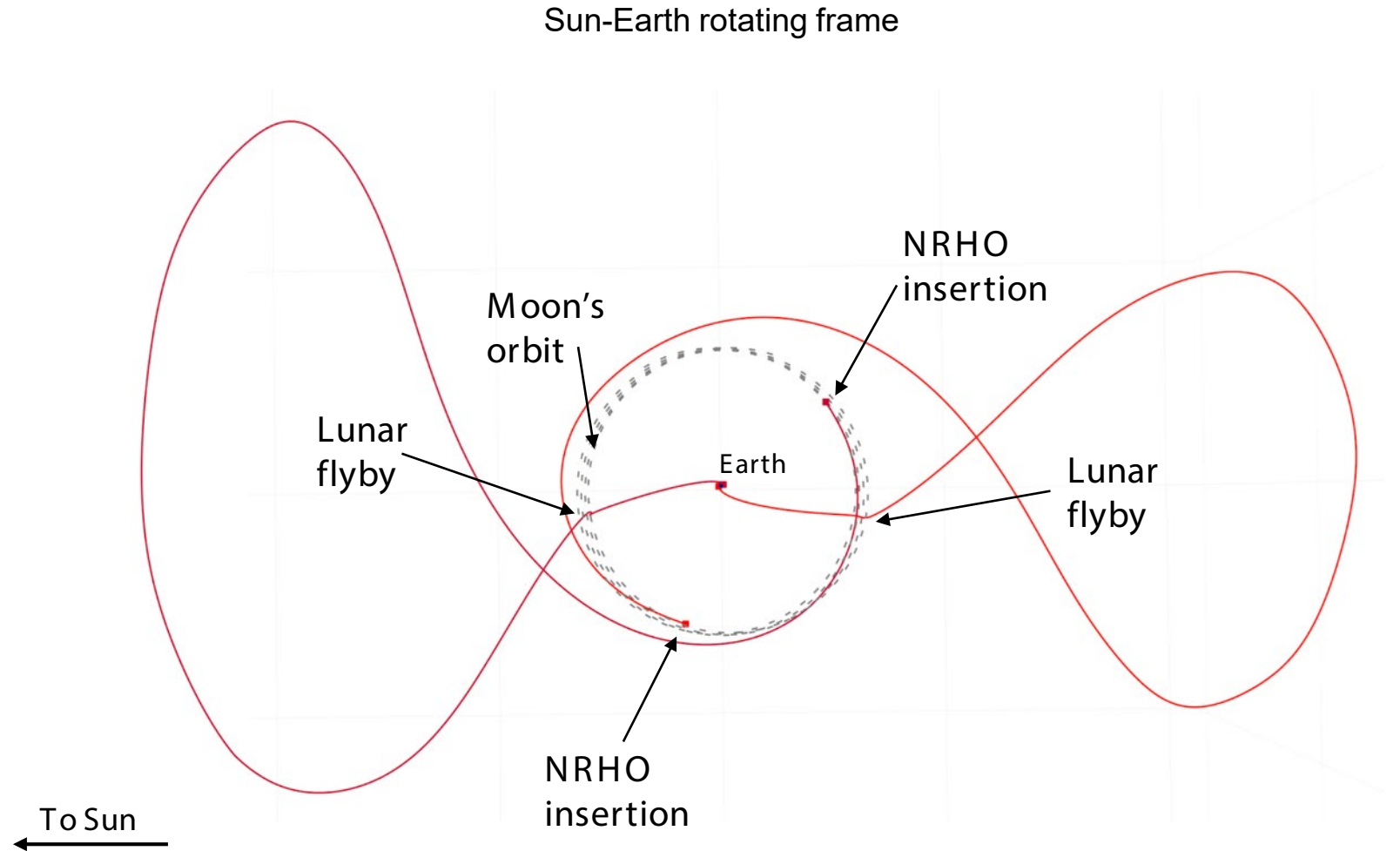
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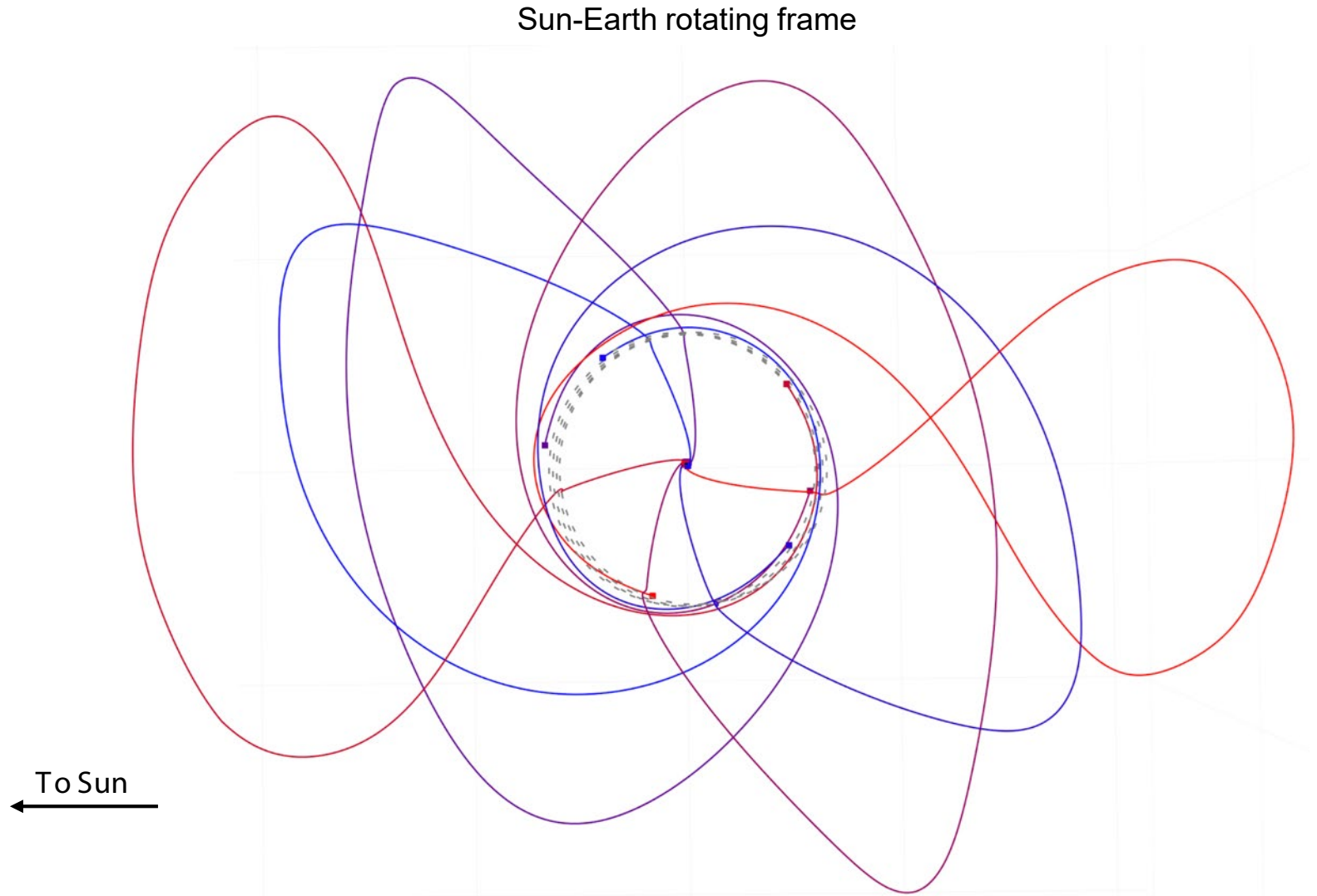
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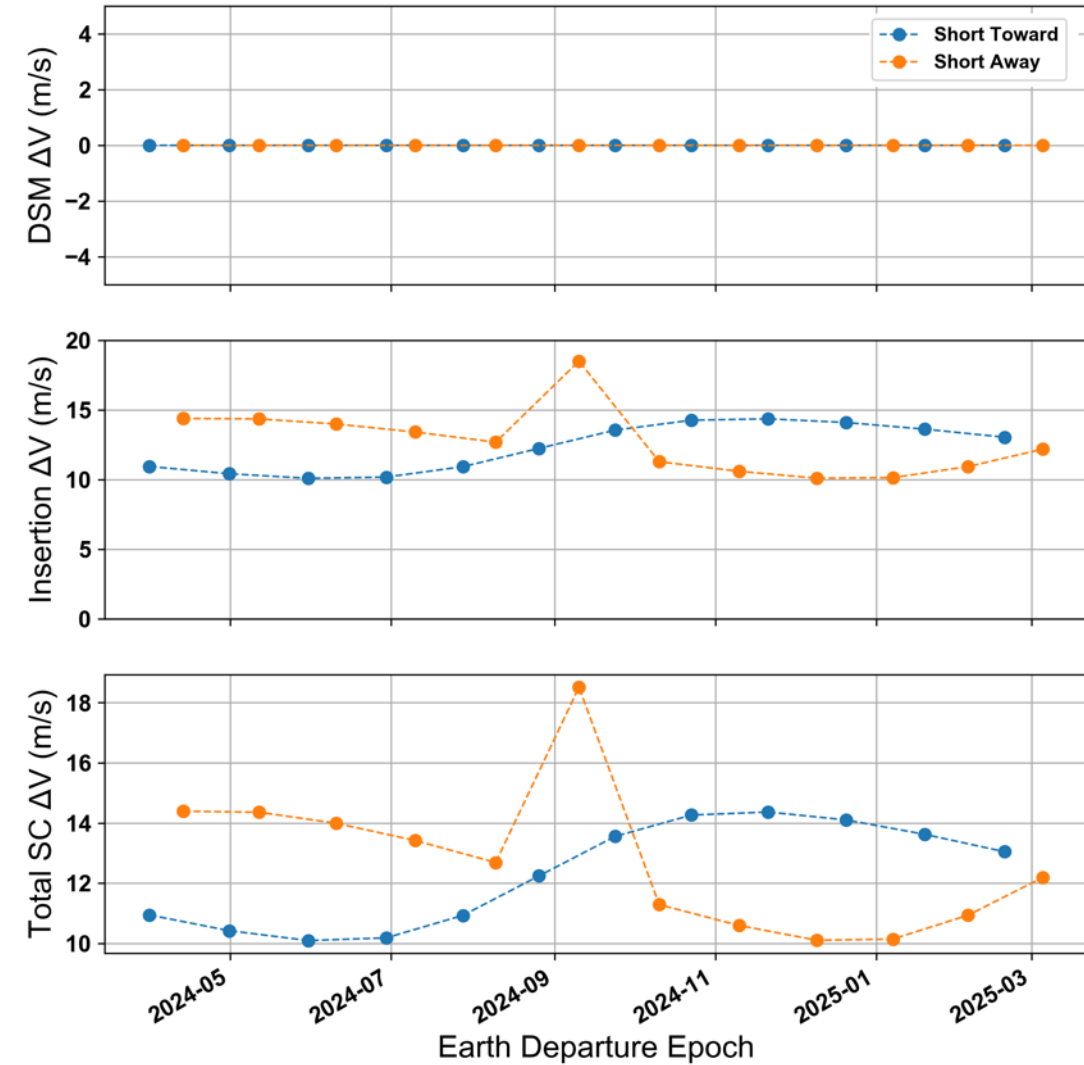
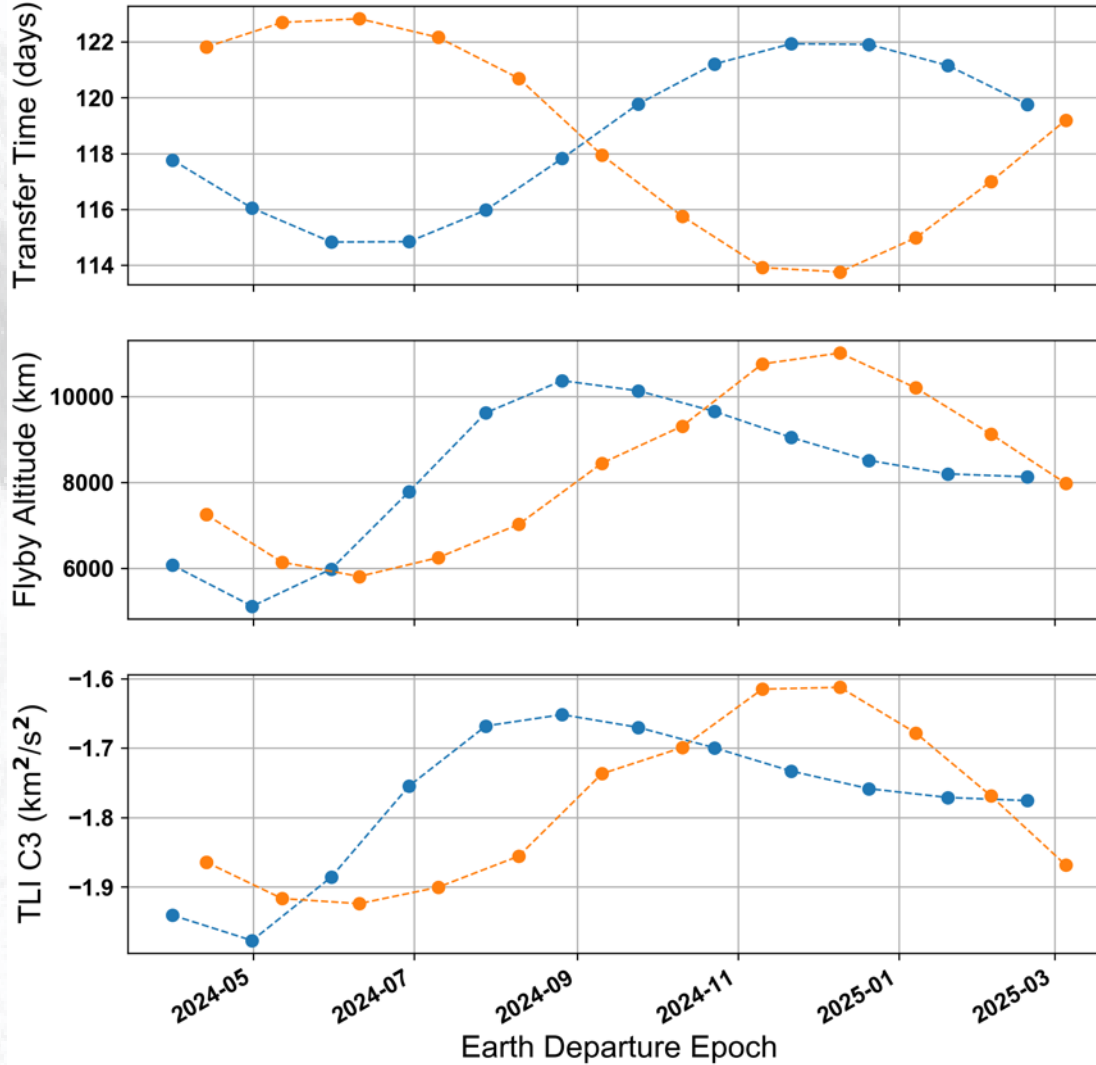


- Families characterized by:
  - “Short”, “Medium”, or “Long” time of flight
    - “Short” transfers: 114-122 days
    - “Medium” transfers: 135-150 days
    - “Long” transfers: 165-173 days
  - Towards or away from the Sun
- Developed 78 seed solutions based on these families
  - Each family, every month for a year
- Then studied launch period of each family

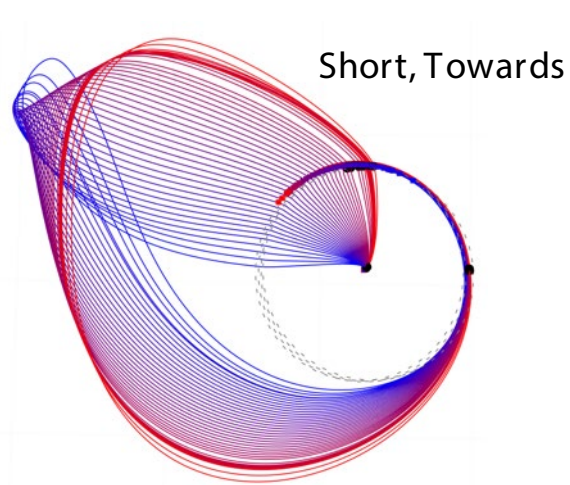
# Phase-Free BLTs with Lunar Flyby



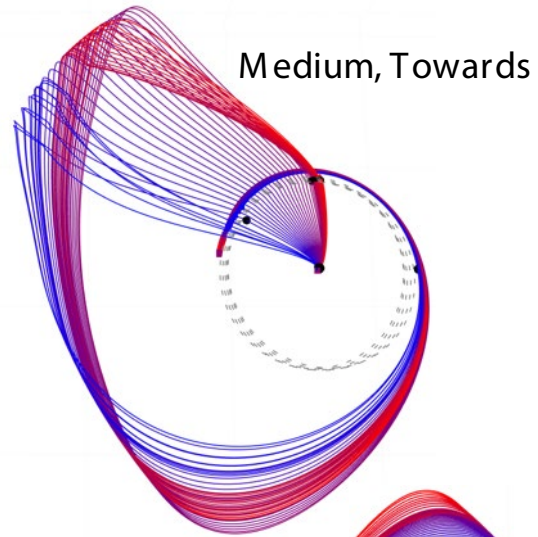
Short Transfers (TOF 114-122 days)



# Phase-Free BLTs with Lunar Flyby

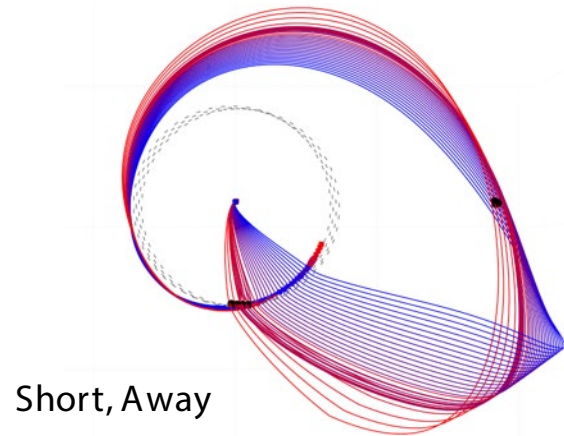


Short, Towards

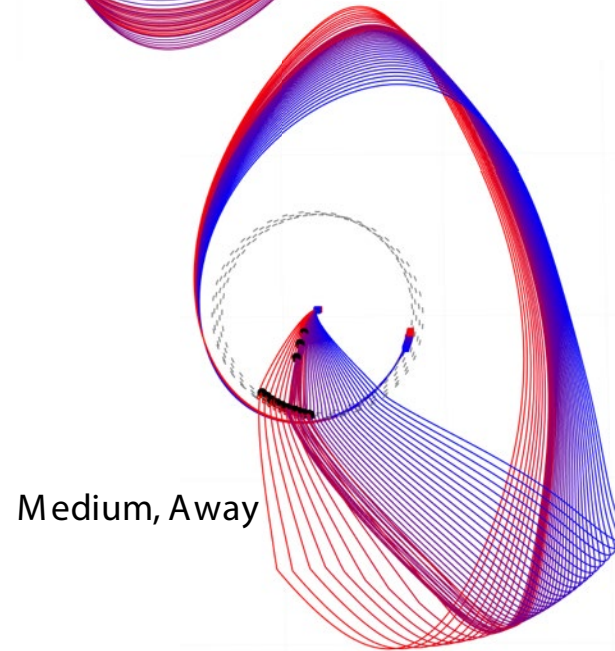


Medium, Towards

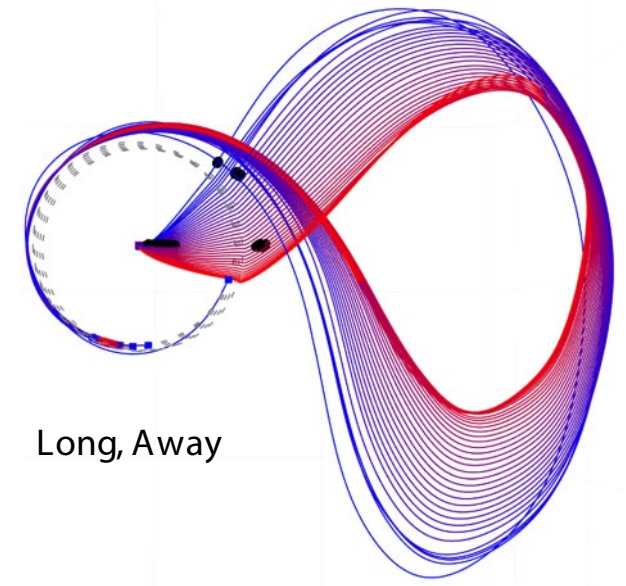
Each of the “seed” solutions used to study the nearby solutions for every family.



Short, Away



Medium, Away



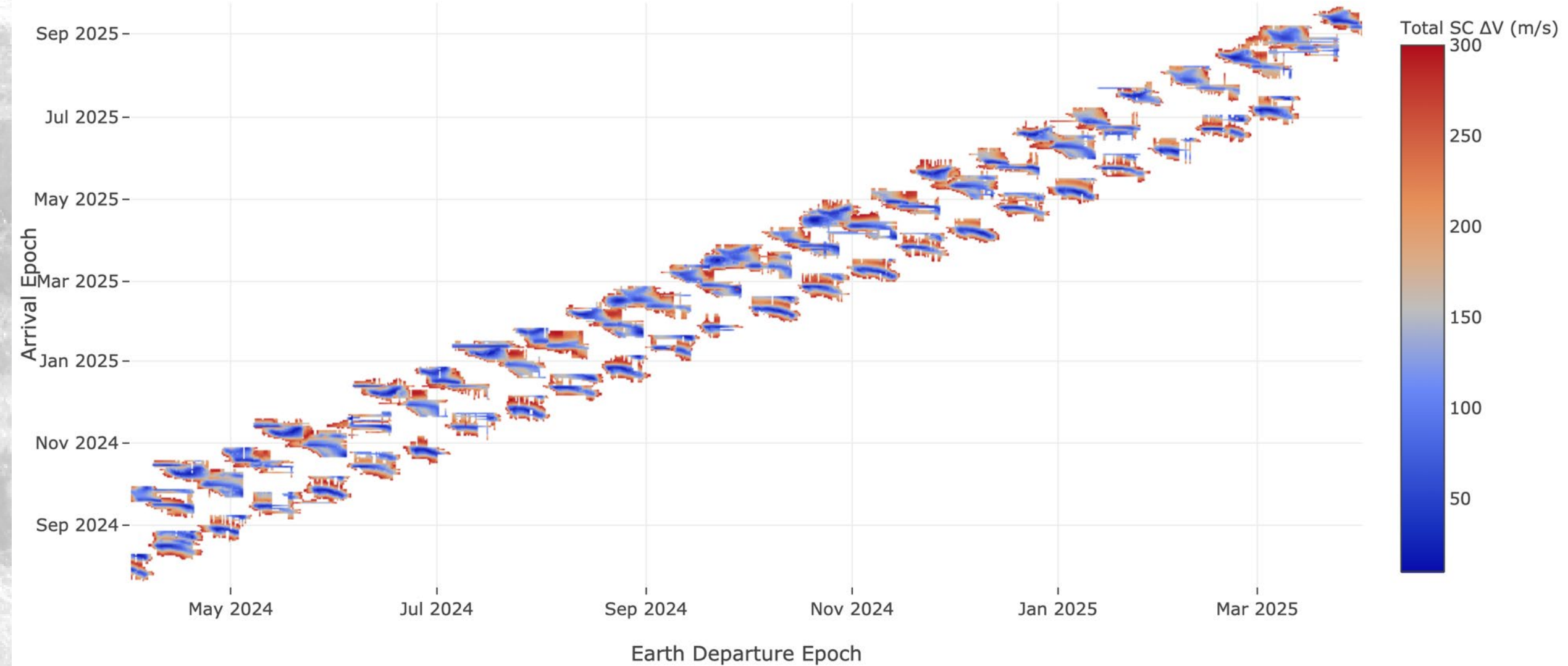
Long, Away

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# Phase-Fixed BLTs with Lunar Flyby



One Year's Worth of Solutions from 6 families

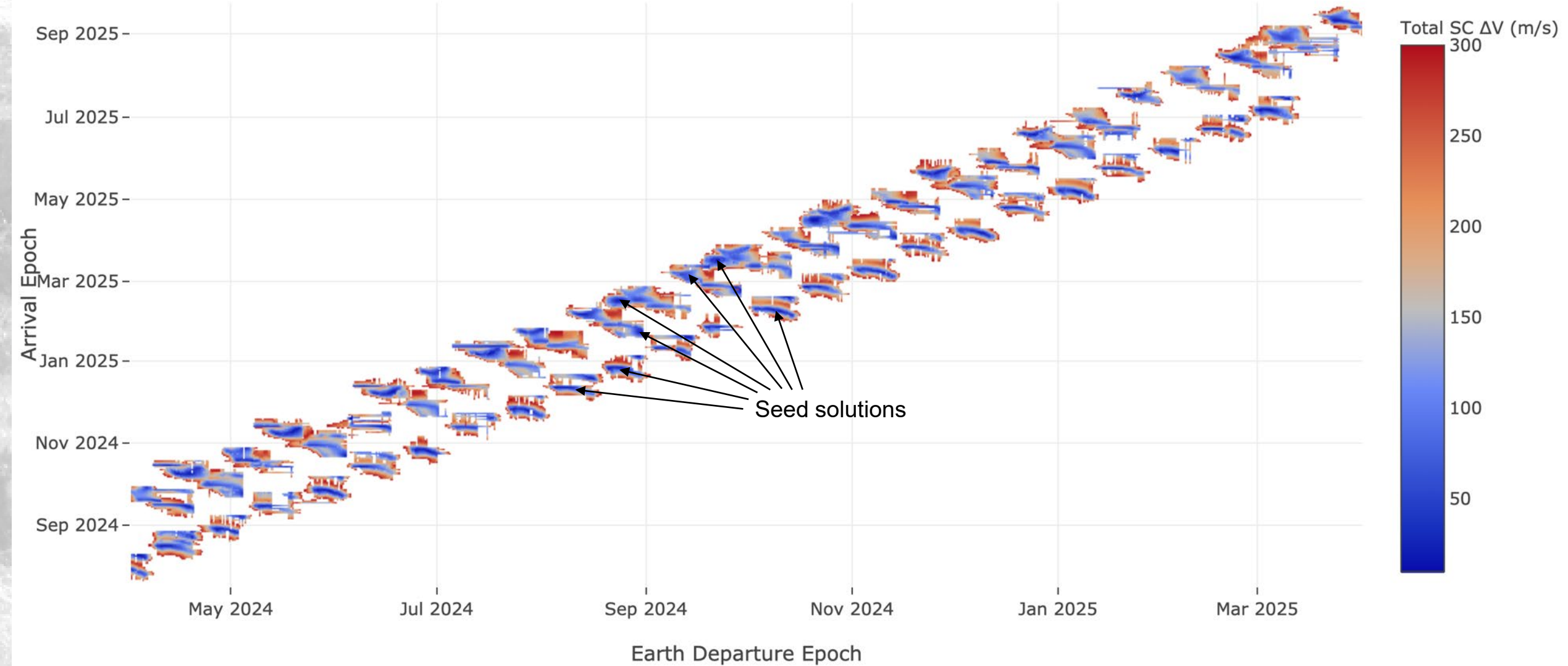




# Phase-Fixed BLTs with Lunar Flyby



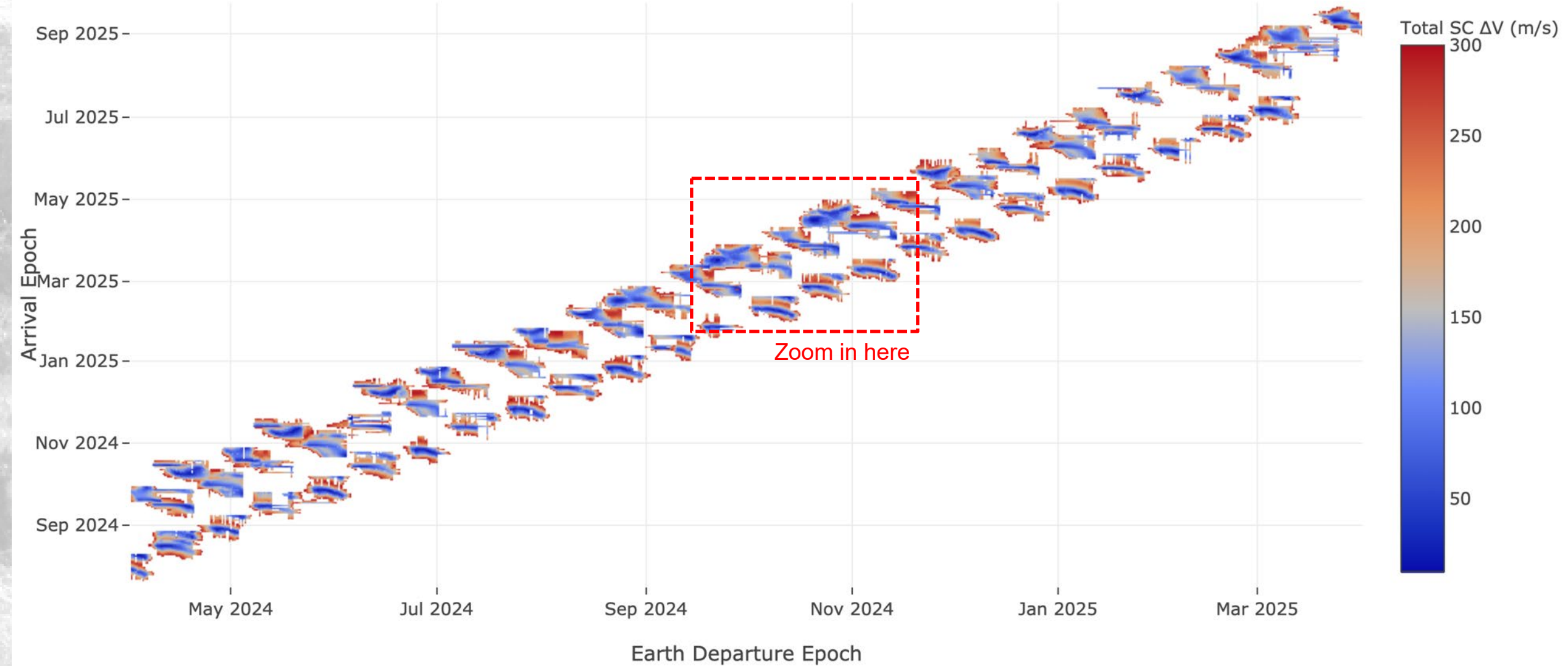
One Year's Worth of Solutions from 6 families



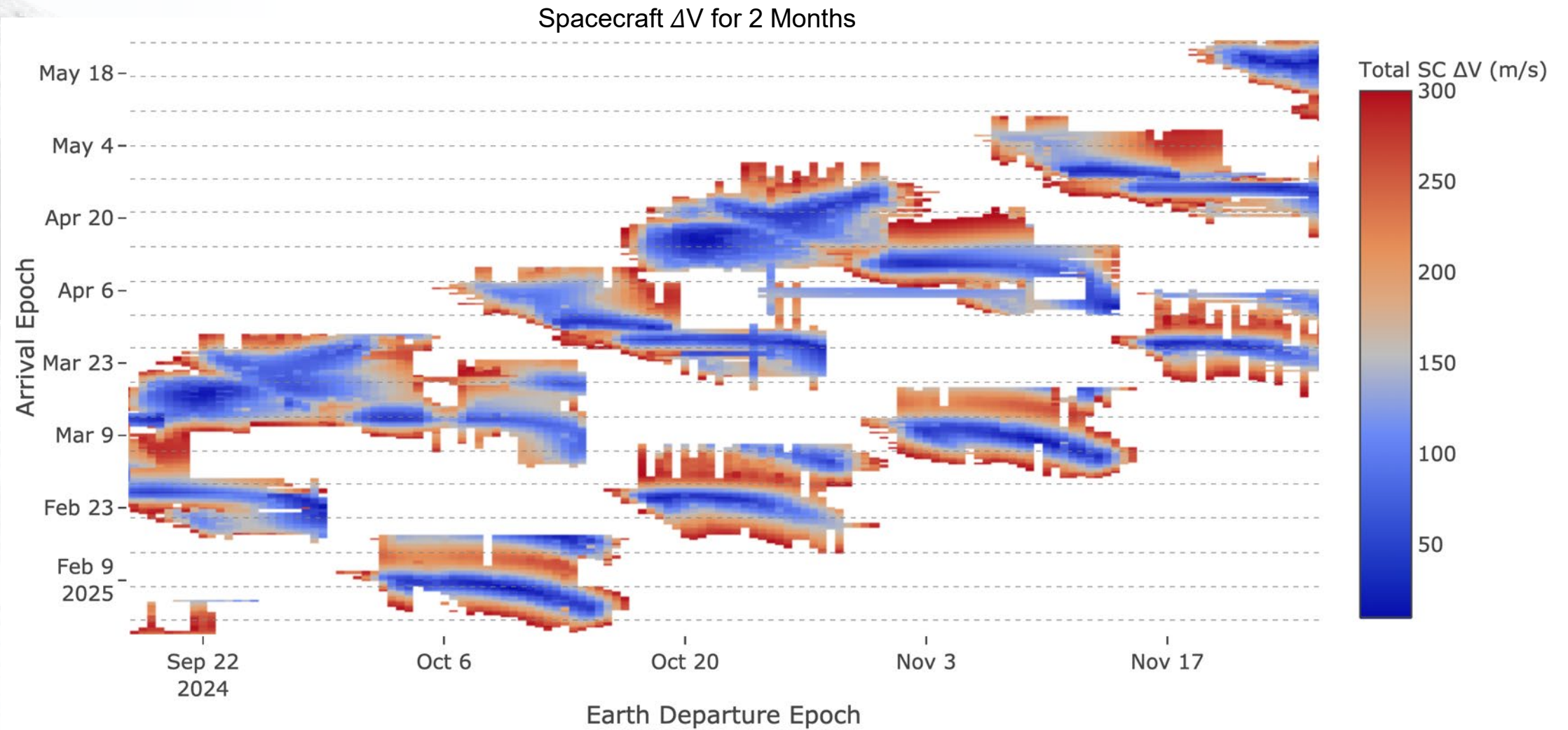


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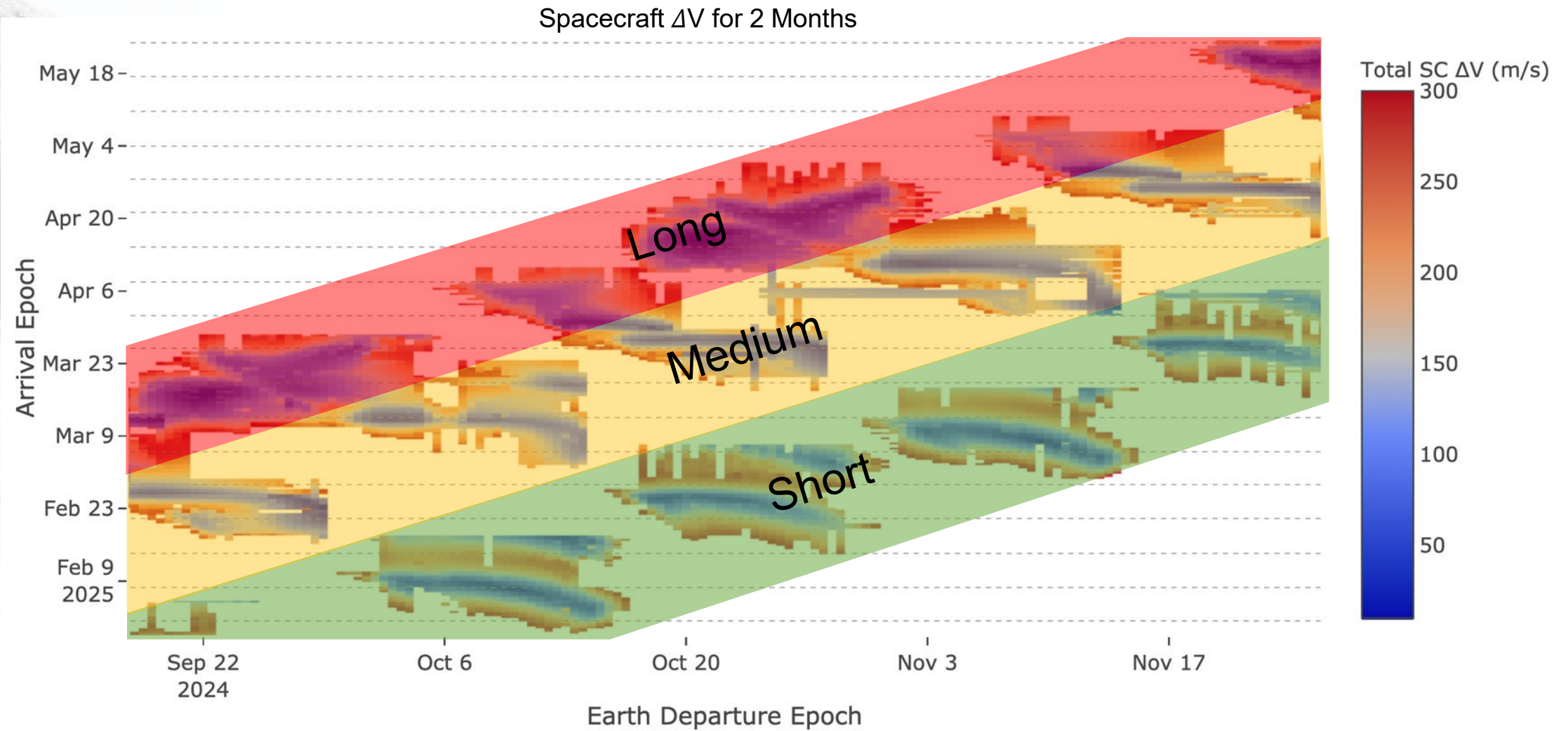
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# Phase-Fixed BLTs with Lunar Flyby

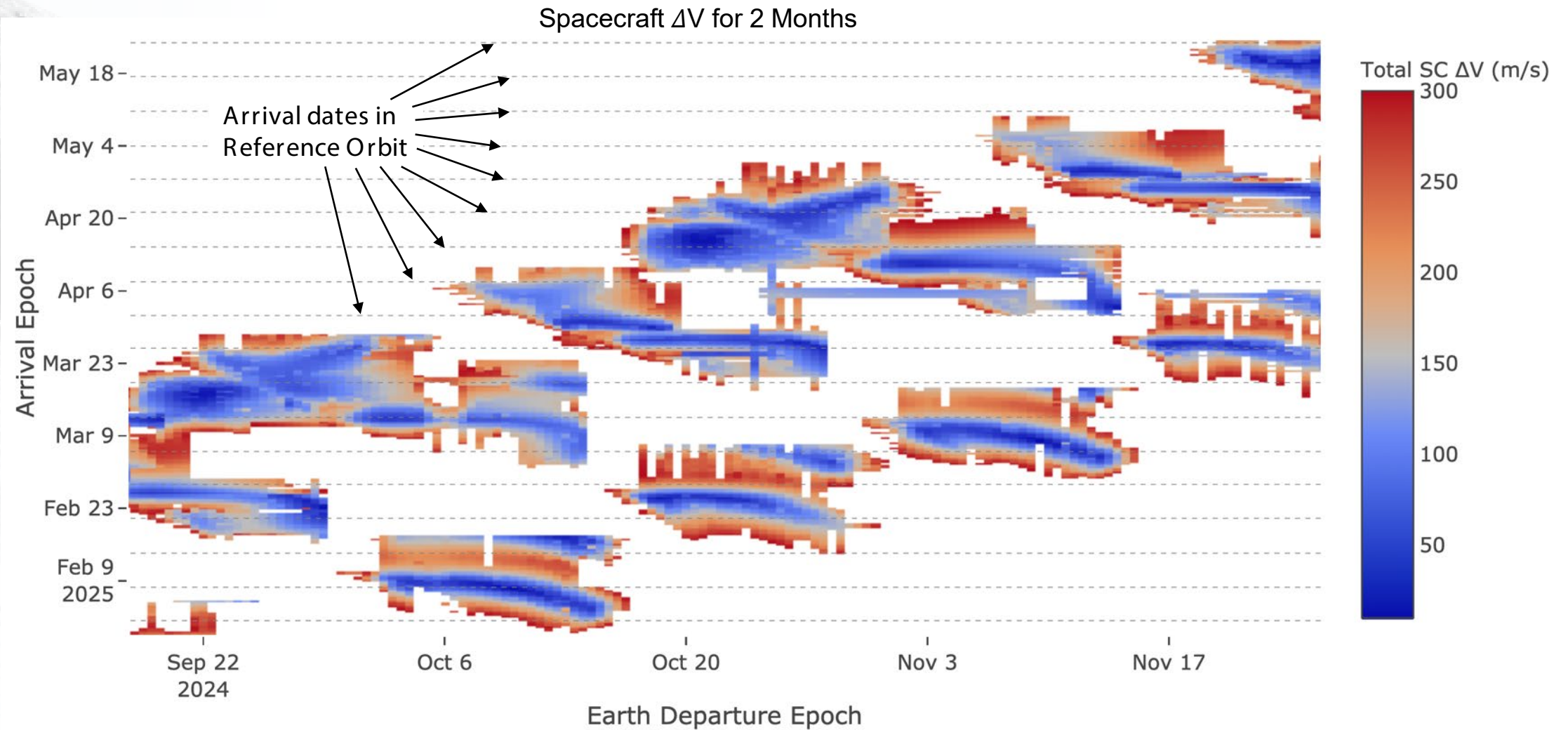


# Phase-Fixed BLTs with Lunar Flyby

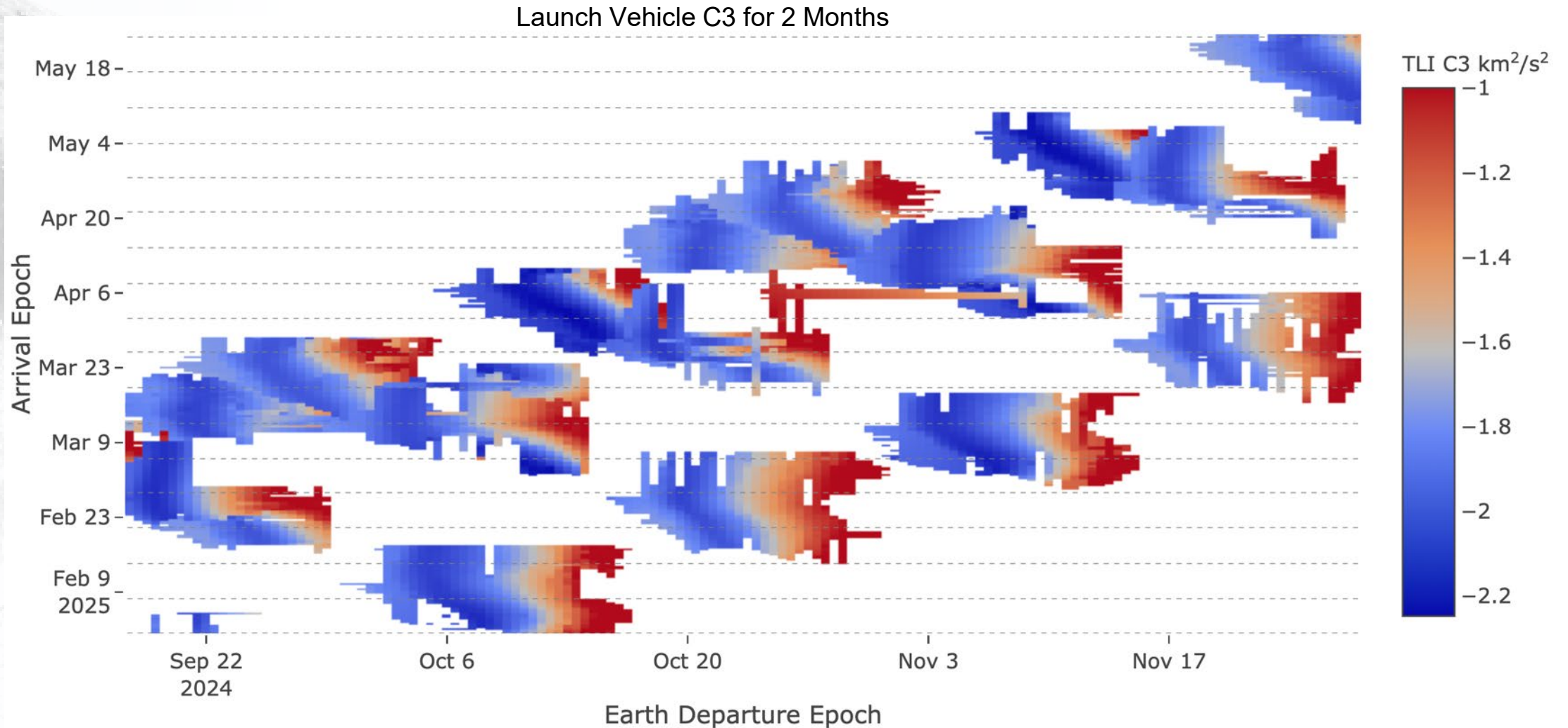




# Phase-Fixed BLTs with Lunar Flyby

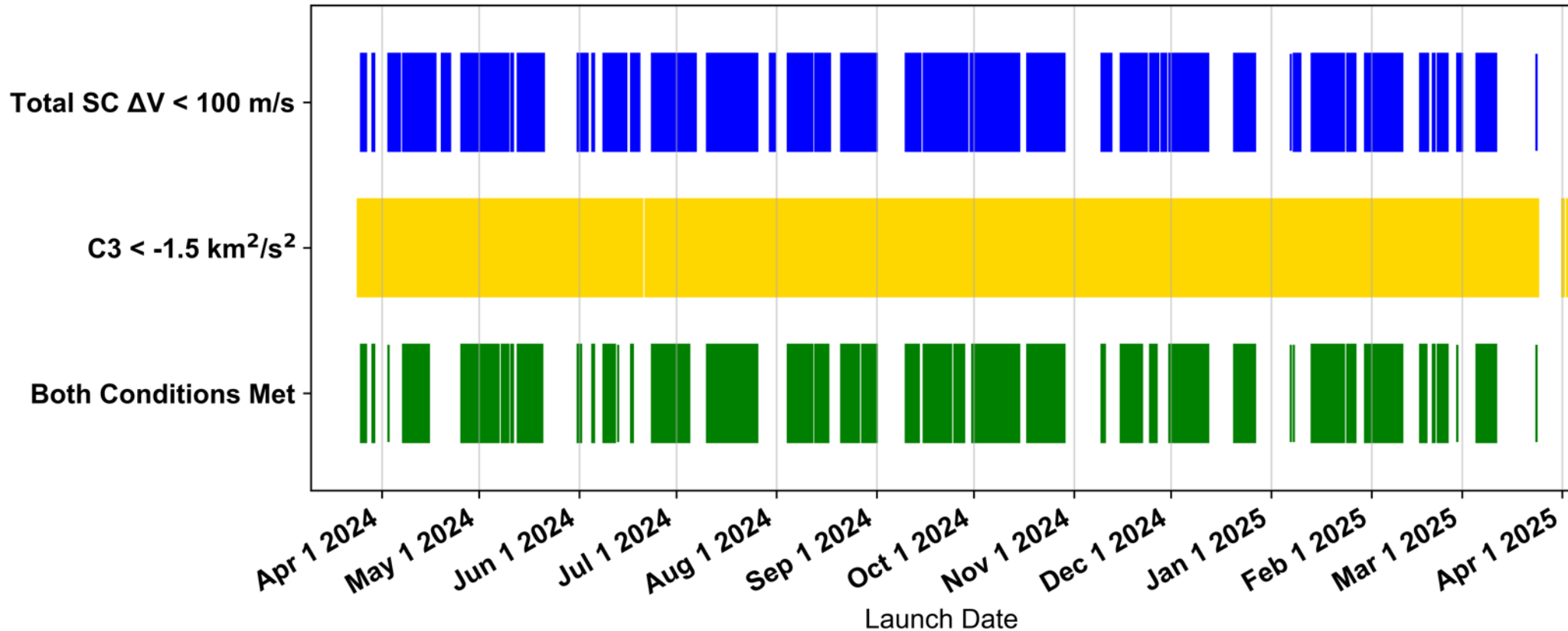


# Phase-Fixed BLTs with Lunar Flyby





# Phase-Fixed BLTs with Lunar Flyby



- Longest interval of no available launch: 12.5 days
- Longest interval of launch available: 15.5 days
- Average interval of launch available: 4.96 days

A large, detailed image of the Moon's surface, showing craters and lunar features, occupies the left side of the slide.

# Recommendations / Conclusions

## Summary

- BLT increases payload delivered to NRHO and reduces spacecraft  $\Delta V$  compared to direct transfer
- Many launch opportunities exist
- Deterministic  $\Delta V$ :
  - Insertion & rendezvous is  $<20$  m/s
  - Launch and spacecraft performance determine deep space maneuvers (DSMs) and launch period availability
- Statistical  $\Delta V$  not analyzed yet, but consists of:
  - Launch vehicle cleanup
  - Trajectory correction maneuvers
  - Rendezvous, proximity operations, and docking
- Time of flight:
  - Without lunar flyby: 12 to 18 weeks
  - With lunar flyby: 16 to 25 weeks
- Launch vehicle C3:
  - BLT without lunar flyby:  $-0.7$  to  $-0.3$  km<sup>2</sup>/s<sup>2</sup>
  - BLT with lunar flyby:  $-2.2$  to  $-1.5$  km<sup>2</sup>/s<sup>2</sup>

Note: These summary values are based on the results to-date with assumptions described.

A large, detailed image of the Moon's surface, showing craters and lunar maria, occupies the left side of the slide.

This study was funded by NASA  
under contract 80NSSC19C0001



Thank you

Contact:

Dr. Nathan Parrish

parrish@advanced-space.com

Additional resources available at

<https://advancedspace.com/blt/>

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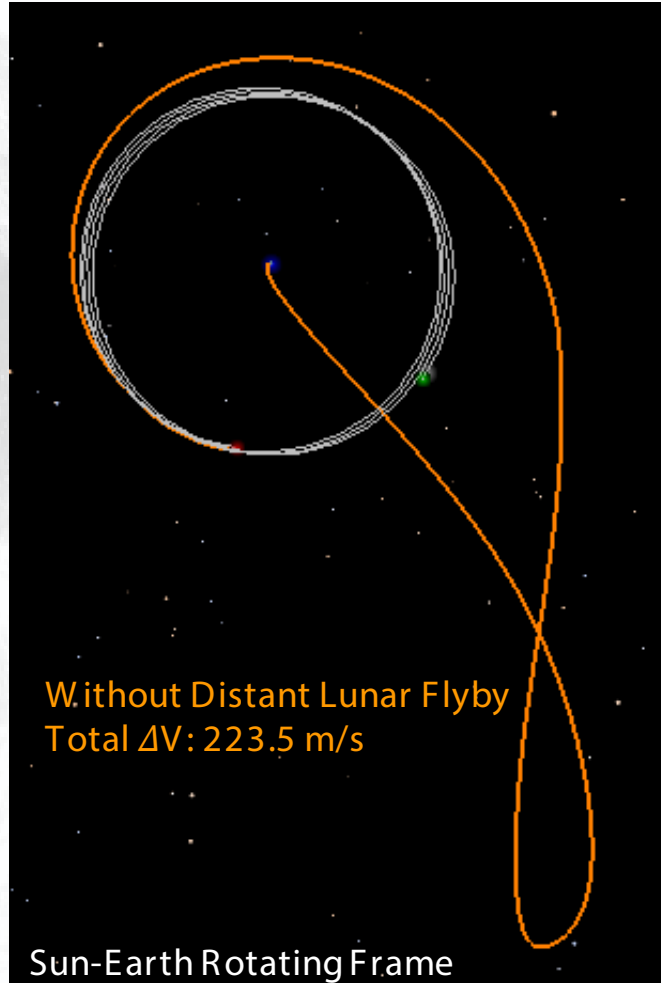
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# Backup



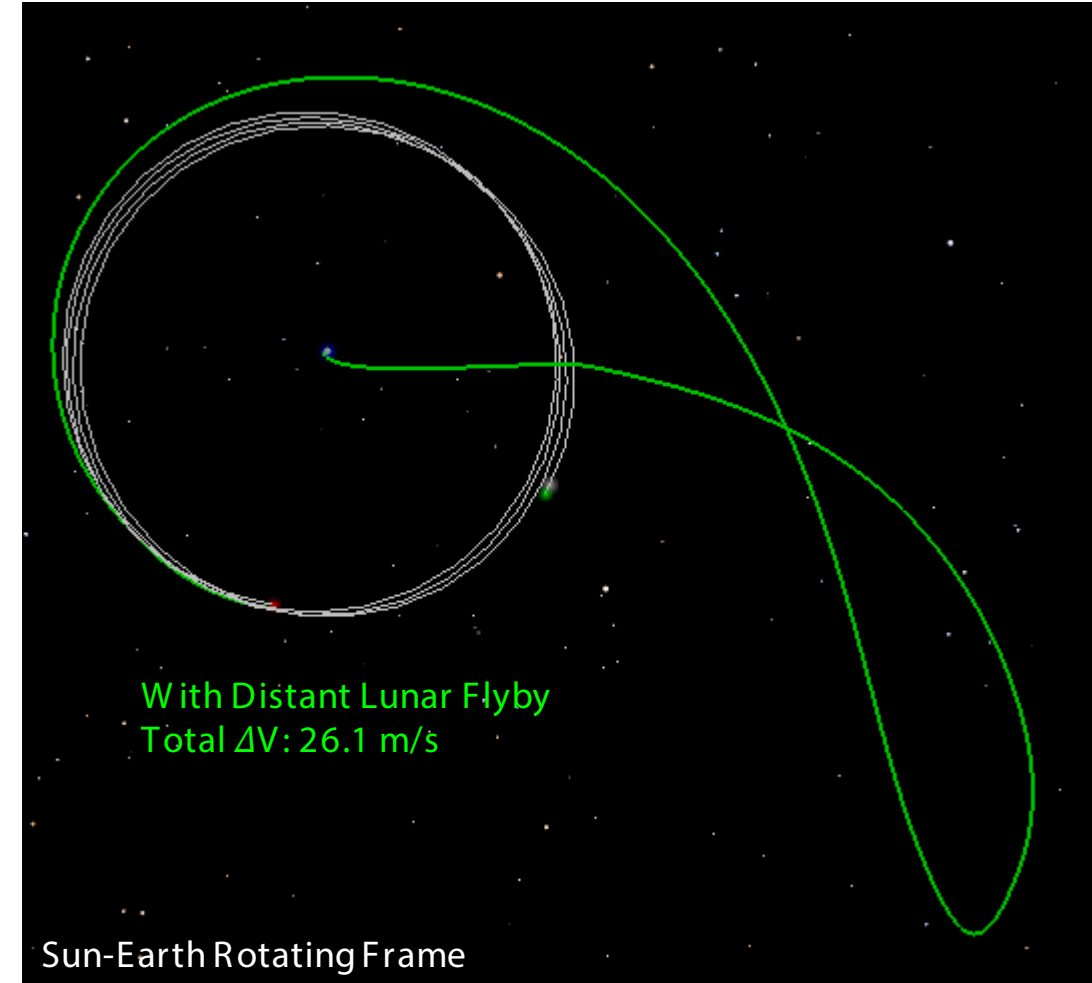
# Phase-Fixed BLTs - Example Simultaneous Options

TLI Epoch: 2024 May 20 12:00



or

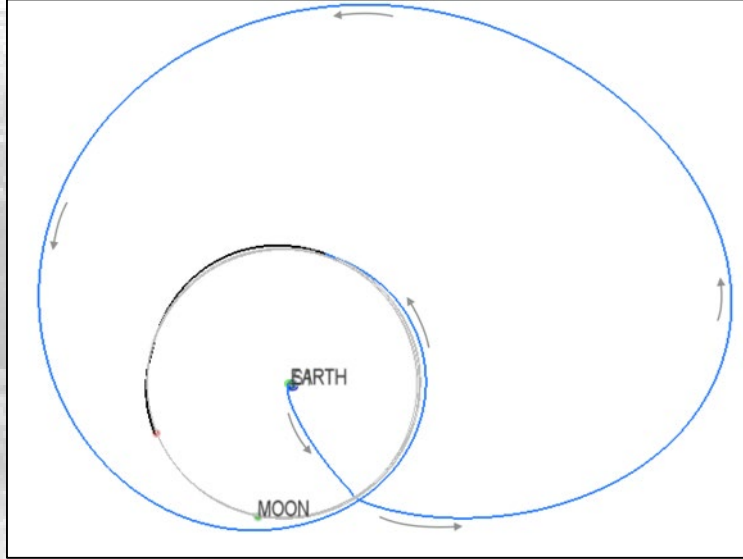
TLI Epoch: 2024 May 21 00:00



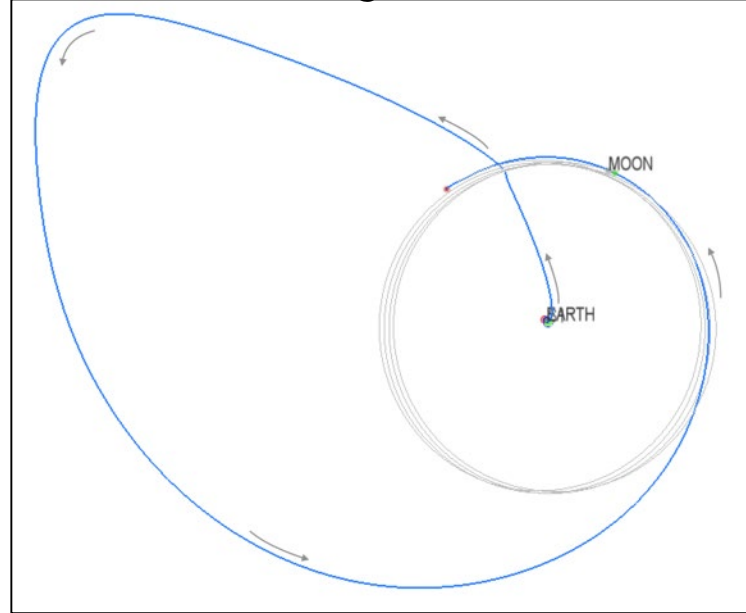
# Summary - Representative Case



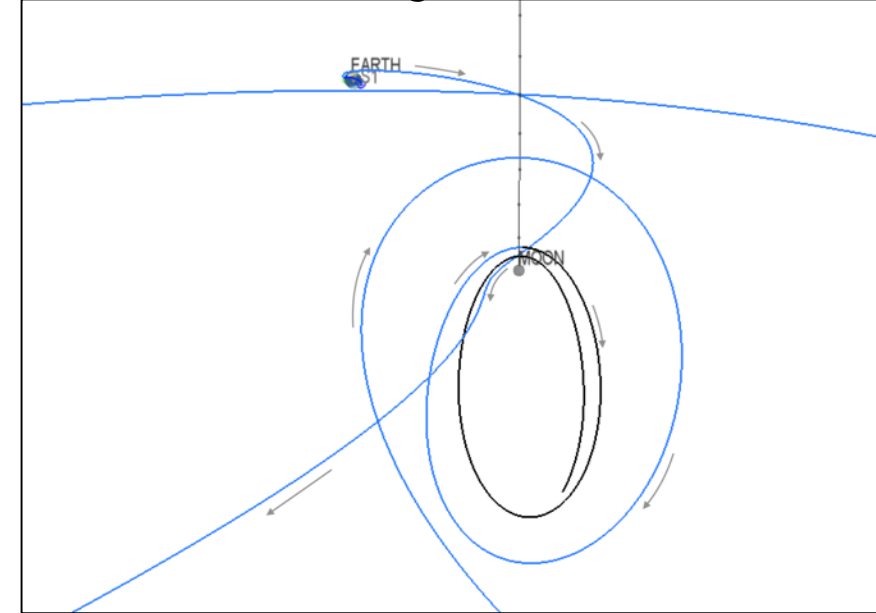
Inertial frame



Sun-Earth rotating frame



Earth-Moon rotating frame



## Characteristics:

- Lunar flyby launch opportunity:  
March 27 - April 4, 2024
- Launch vehicle C3 requirement:  $-1.4 \text{ km}^2/\text{s}^2$
- Spacecraft  $\Delta V$  budget (DSMs & insertion): 60 m/s
- Time of flight: 127-115 days
- Flyby altitude: 200-11,000 km

## Caveats:

- Launch period is based on phase-free case. Constraining final rendezvous will reduce the launch period and/or increase  $\Delta V$  required.
- Simplified spacecraft model.
- Additional analysis required to evaluate statistical  $\Delta V$ .

